Dynamics of core-mantle separation: Influence of viscosity contrast and metal/silicate partition coefficients on the chemical equilibrium

V. Clesi, J. Monteux, B. Qaddah, M. Le Bars, J.-B. Wacheul, Mohamed Ali
M.A. Bouhifd

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5 V. Clesi[a,*], J. Monteux[a], B. Qaddah[a,b], M. Le Bars[b], J.-B. Wacheul[b], M.A. Bouhifd[a]

6

7 [a]Université Clermont Auvergne, CNRS, IRD, OPGC, Laboratoire Magmas et Volcans, F-63000 Clermont-

8 Ferrand, France

9 [b]CNRS, Aix Marseille Université, Centrale Marseille, Institut de Recherche sur les Phénomènes Hors

10 Equilibre, UMR 7342, 49, Rue F. Joliot-Curie - B.P. 146, 13384 Marseille Cedex 13, France

11

12 *Corresponding author: vincent.clesi@univ-lyon1.fr

13 Present address: Laboratoire de Géologie de Lyon- Terre, Planètes, Environnement, CNRS UMR

14 5276, ENS de Lyon, Université Lyon 1. Campus de la Douà, Batiment Geode, 2 Rue Raphaël

15 Dubois, 69622 Villeurbanne Cedex.

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Abstract

20   The composition of the Earth's core and mantle is set by the chemical equilibrium between metals

21   and silicates during core/mantle segregation. The metallic core separated from the mantle by

22   gravitational descent in the form of diapirs in a magma ocean, and therefore the dynamics of the

23   diapir's downward movement has an influence on the chemical equilibrium. In this study, we

24   characterize the descent of metallic droplets into a molten silicate using numerical models. By

25   varying the silicate and metal viscosities (between 0.1 and 1000 Pa.s for each phase) as well as

26   the partition coefficient between metal and silicate ($D^{met/sil}$, varying between 1 and 1000), we

27   obtained quantifying parametrizing equations for the degree of equilibrium between molten metal

28   and molten silicate, in a regime characterized by low *We* (*We* < 10) and low *Re* (10^{-3}<*Re*<10^{2}).

29   We showed that the main parameters controlling the equilibrium for a siderophile element are the

30   viscosity of the silicate and the partition coefficient. We applied our parameterization for Ni and

31   Co in the context of late accretion on Earth so as to quantify the variation of the Ni/Co ratio after

32   a large impact as a function of the magma ocean viscosity, for an iron-rain scenario of

33   metal/silicate segregation. Using previous models (Canup, 2004) of the Moon–forming impact,

34   we showed that the Moon formation had an effect on the current Ni/Co ratio. Depending on the

35   radius of Theia's core and the viscosity of the magma ocean produced after the impact between

36   the proto-Earth and Theia, the Moon formation could account for 0.45 % to 3 % of the current

37   Ni/Co ratio for magma ocean viscosities of 0.1 to 100 Pa.s, respectively.

38

39

1. Introduction

The main process occurring on Earth during the first 100-150 million years was the segregation of its metallic Fe-rich core (*e.g.* Bouhifd et al., 2017; Rubie et al., 2015; Wood et al., 2006; and references therein). One major consequence of this segregation is the depletion of the Earth's mantle in the siderophile elements relative to primitive solar system abundances (*e.g.* Jones and Drake, 1986).

The most recent Earth core formation models include a combination of multistage core-mantle differentiation with N-body accretion simulations, combined with continuous Earth core formation where pressure, temperature, oxygen fugacity and chemical composition of both the mantle and core vary during accretion of the Earth (*e.g.* Rubie et al., 2015, and references therein). These models consider that the accretion of the Earth occurred during a series of large impact events (*e.g.* Canup, 2008; Wetherill, 1985; O'Brien et al., 2006; Monteux et al., 2009; Nakajima and Stevenson, 2015). More importantly, these models provide results for the metal-silicate partitioning of a significant number of siderophile elements, which are consistent with observed mantle abundances given that the oxygen fugacity increases from about IW-5 to IW-2 (5 to 2 log units lower than the Iron-Wüstite buffer) during core segregation (*e.g.* Cartier et al., 2014; Rubie et al., 2015; Wade and Wood, 2005).

In this context, the behavior of Ni and Co (two refractory and moderately siderophile elements) has been considered to provide an important indication of the conditions of

60   Earth core formation. The consensus is now that metal-silicate equilibration at high

61   pressure, in the range of 40 – 60 GPa (corresponding to depths of 1000 – 1500 km), was

62   required to produce the observed Ni and Co depletions in the mantle (Bouhifd and

63   Jephcoat, 2011; Siebert et al., 2012; Righter, 2011; Fischer et al., 2015; Clesi et al., 2016,

64   for some of the most recent studies). Similar conclusions were reached based on the metal-

65   silicate partitioning of lithophile and weakly-siderophile elements (*e.g*. Mann et al., 2009).

66   One can note here that the conditions of Earth core formation as derived from metal-

67   silicate partitioning of several elements cannot be used as an argument for single-stage

68   core formation. This is highly unlikely given that Earth core formation occurred over a

69   series of large impact events.

70   Most core formation models are based on metal-silicate partitioning experiments

71   where both phases are fully molten and both thermodynamic and kinetic equilibrium are

72   reached. This type of scenario favors rapid core - mantle segregation, which is confirmed

73   by isotopic studies on Hf/W and short lived isotopes (Kleine et al., 2002; Jacobsen et al.,

74   2008). If the kinetic equilibrium is well constrained, the extent to which the mantle and

75   core equilibrate with each other is model dependent. So we know that if the metal were to

76   segregate by forming large diapirs descending through the silicate magma ocean, the

77   timescale for the equilibration would be too long to explain the isotopic ratios of Hf/W

78   (Rubie et al., 2003). Therefore, the metal could have segregated by forming smaller

79   diapirs, or droplets, whose radius varied between 0.1 to 10 cm, forming a cloud of iron in

80   the magma ocean (Deguen et al., 2014; Wacheul et al., 2014). An intermediate scenario

81   combining iron-rain mingling for the first part of segregation in the magma ocean,

82   followed by creation of large descending diapirs also exists, which can explain the

83   equilibrium in a deep magma ocean. In such a scenario, the metal falls through the molten

84   silicate in the form of droplets, and then forms a metallic pond at the base of the magma

85   ocean. Gravitational instability then allows metal to form large diapirs which descend

86   through the solid layer of the mantle into the proto-core (*e.g*. Stevenson, 1981, Monteux

87   et al., 2015, Fleck et al., 2018). This study focuses on the iron-rain phase of core-mantle

88   segregation, during which chemical equilibrium is reached (Rubie et al., 2003, 2011), as

89   large diapirs have less chemical interaction with the surrounding fluid (Ulvrova et al.,

90   2011; Wacheul et al., 2014). In the scenario of segregation by iron rain (Fig. 1), the extent

91   to which the magma ocean is in equilibrium with the core depends on the properties of the

92   metallic flow. The physics of the fluid flow is dependent on various parameters, one of the

93   most important being the viscosity of the surrounding fluid (Ke and Solomatov, 2009;

94   Monteux et al., 2009; Ricard et al., 2009). Numerical and analog simulations of a metallic

95   diapir descending through a surrounding fluid with different viscosities have shown that

96   the diapir is more stable when surrounding viscosity increases from low values ($\sim 10^{-1}$

97   Pa.s) to high values (~ 100 Pa.s), (Samuel, 2012; Wacheul et al., 2014). This has an impact

98   on chemical equilibrium, since break–up of the diapir increases the surface of exchange

99   between metal and silicate and small droplets sink more slowly than large diapirs (Ulvrova

100 et al., 2011; Wacheul et al., 2014). The efficiency of equilibrium is also increased when

101 internal convection favors homogenization of concentrations in the metallic droplets

102 (Ulvrova et al., 2011).

103   The goal of the present study is to characterize the influence of viscosity (metal and

104 silicate phases) and chemical equilibrium on the global equilibrium rate in a magma ocean.

105 To do that, the most relevant methods are analog and numerical modeling (e.g. Samuel

106 and Tackley, 2008; Sramek et al., 2010; Deguen et al., 2011; Wacheul et al., 2014).

107 Numerical simulations are more practical than analog ones for studying the effects of

108 different phenomena happening simultaneously. In addition, it is difficult to find analogs

109 for both metal and silicate which will react exactly like these two phases, and even more

110 complicated to find analogs that behave chemically and physically in the same way as

111 molten metal and molten silicate. Given the limitations of analog experiments for multiple

112 physical modeling, we chose to perform numerical simulations of a falling metallic sphere

113 into a molten silicate using COMSOL Multiphysics 5.0 modeling software. This approach

114 allows the chemical equilibrium for different types of siderophile elements to be

115 determined. In our simulations we combined chemical diffusion calculations with different

116 types of flow. In particular, these simulations led us to explore the contamination of a

117 silicate column by an excess of a siderophile element initially present in the diapir. Since

118 viscosity influences the type of flow, which in turn is crucial in core-mantle equilibrium

119 modeling (Rubie et al., 2003; 2011; Samuel, 2012), viscosity must have an influence on

120   the extent of core-mantle equilibrium. Furthermore, the equilibrium depends on the

121   partition coefficients of the elements between metal and silicate ($D^{met/sil}$), which depend

122   on pressure, temperature, oxygen fugacity and composition of metal and silicate.

123   Therefore, we tested the contamination of silicate by generic siderophile elements using

124   four different values of $D^{met/sil}$ (1, 10, 100, 1000).

125   Since major chemical transfers likely occurred during the iron rain process (Rubie et

126   al., 2003) our simulations looked at the equilibrium of droplets with the surrounding

127   silicate. In general, large diapirs in a turbulent environment tend to break into small

128   droplets, forming a cloud in which each droplet moves at the same speed (Wacheul and

129   Le Bars, 2017, 2018). In this study, we look at how one droplet of a given radius (R_{Fe} = 1

130   cm), which can be deformed but cannot break (see Wacheul et al., 2014), interacts with

131   the surrounding silicate. Then this behavior is extrapolated to the entire droplet cloud, and

132   we can estimate the extent to which equilibrium is reached between the magma ocean and

133   the falling metal during planetary accretion.

134   As a result of these simulations, we constrain the chemical exchanges between a small

135   metallic diapir and a silicate volume as a function of silicate viscosity (varying from 0.1

136   Pa.s to 1000 Pa.s), the viscosity ratio between metal and silicate, and time. We thus

137   parameterize the effect of varying viscosity on metal-silicate equilibration, and we use this

138   parameterization to re-evaluate models of core-mantle segregation. Moreover, we

139   characterize the effect of changing the magma ocean viscosity on the chemical

140 composition of the mantle. Finally, we discuss the potential consequences of giant impacts

141 such as the Moon-forming impact on the chemical composition of the Earth's mantle.

142

143 **2. Physical Model**

144   To model the sinking of a metallic droplet into a silicate liquid, we used the software

145 COMSOL Multiphysics, and in particular the modules "Computational Fluids Dynamics"

146 and "Chemical Reaction Engineering". In each module, a set of equations is defined and

147 solved at each time step. These equations are described in the following subsections. The

148 parameters we used for these equations are listed in Table 1.

149

150 **2.1. Two-phase flow model**

151   In our study, the fluid dynamics are governed by the Navier-Stokes equations that

152 characterize:

153   • Conservation of mass

154 $$\nabla \cdot \boldsymbol{u} = 0 \tag{1}$$

155   • Conservation of momentum

156 $$\rho \frac{\partial \boldsymbol{u}}{\partial t} + \rho(\boldsymbol{u} \cdot \nabla)\boldsymbol{u} = -\nabla P \boldsymbol{I} + \nabla \cdot [\mu(\nabla \boldsymbol{u} + (\nabla \boldsymbol{u})^T)] + \rho \boldsymbol{g} + \boldsymbol{F_{st}} \tag{2}$$

157

158   Equation 1 is the conservation of mass for an incompressible fluid with $\boldsymbol{u}$ the flow

159   velocity **vector**. Equation 2 describes the conservation of momentum, with acceleration of

160   the fluid $(\frac{\partial \boldsymbol{u}}{\partial t})$ and an inertia term $(\rho(\boldsymbol{u} \cdot \nabla)\boldsymbol{u})$ where ρ is fluid density. The first term on

161   the right-hand side of Eq. 2 $(-\nabla P)$ is the effect of the dynamic pressure P on the fluid.

162   The second term $(\nabla \cdot [\mu(\nabla \boldsymbol{u} + (\nabla \boldsymbol{u})^T)])$ is the component representing the effect of

163   viscous forces on the fluid with μ the fluid viscosity. The third term $(\rho \boldsymbol{g})$ is the

164   gravitational force that applies to the whole domain with $\boldsymbol{g}$ the gravitational acceleration

165   **vector**. The fourth term $\boldsymbol{F_{st}} = \nabla \cdot (\sigma(\boldsymbol{I} - \boldsymbol{nn}^T)\delta)$ is the surface tension force with σ the

166   surface tension coefficient, $\mathbf{I}$ the identity matrix, $\boldsymbol{n}$ a unit vector normal to the surface of

167   interest and δ a smeared out Dirac function located at the interface. Since the volume of

168   metal is small, we ignored the Coriolis forces in Eq. 2.

169   We monitored the interface between the liquid iron droplet and the molten silicates using

170   the Level Set method, a Eulerian and implicit method used in multiphase flow problems

171   (e.g. Qaddah et al., 2019). For that, we defined a function Φ, characterizing the silicate

172   when $\Phi = 0$ and the metal when $\Phi = 1$. The boundary between the two phases was then

173   set at $\Phi = 0.5$. These values were obtained by modifying the level set field using a smeared

174   out Heaviside function (Olsson & Kreiss, 2005), which allows direct calculation of the

175   volume fraction of a given phase by integration of the variable Φ on the volume

176   considered. The equation governing the transport of Φ is:

177

178 $$\frac{\partial \Phi}{\partial t} + \boldsymbol{u} \cdot \nabla\Phi = \gamma\nabla\left(\epsilon_{ls}\nabla\Phi - \Phi(1-\Phi)\frac{\nabla\Phi}{|\nabla\Phi|}\right) \tag{3}$$

179

180   with γ (m/s) and ϵ_{ls} (m) the reinitialization parameters. The γ parameter limits the

181   numerical diffusion of the metallic phase during the simulation and needs to be adjusted

182   empirically when the viscosity varies. Indeed, γ is a parameter that determines the amount

183   of reinitialization or stabilization and must be carefully adjusted for each specific problem.

184   If γ is too low, the thickness of the interface might not remain constant, and oscillations in

185   Φ could appear because of numerical instabilities. On the other hand, if γ is too high, the

186   interface moves incorrectly. The ideal value of γ was given by the maximum velocity

187   reached by the diapir during its descent, as detailed in section 3. The range of values for γ

188   is given in Table 1. ϵ_{ls} is the parameter controlling the width of the interface between

189   fluids during reinitialization. This equation (Eq. 3) is a combination of the equations

190   presented in Olsson & Kreiss (2005), modified for the COMSOL in-built solver. This

191   solver allows the advection (on the left-hand side of the equation) and the reinitialization

192   parameter (right-hand side of the equation) to be solved at the same time. The dynamic

193   viscosity and the density are evaluated using the level set function and are defined by $\mu =$

194    $\mu_{sil} + \Phi(\mu_{met} - \mu_{sil})$ and $\rho = \rho_{sil} + \Phi(\rho_{met} - \rho_{sil})$, respectively (subscript *met* refers

195   to metal and *sil* to silicates). The resolution of the level set equation without using the

196   COMSOL Multiphysics module is detailed in Olsson & Kreiss, 2005. Furthermore, this

197   method has been already validated and applied to a similar problem in Qaddah et al., 2019.

198

199   The temperature of both the metallic droplets and the surrounding molten silicates is

200   difficult to constrain. It is related to the history of both phases before the merging and

201   involves radioactive heating, viscous dissipation and accretionary heating. In our study

202   we consider that the impact that precedes the iron droplet sinking homogenizes the

203   temperature of both phases. Hence, we do not consider heat conservation in the equations

204   solved in our models, and focus instead on the chemical equilibration processes alone.

205

206

207   **2.2.** *Chemical model*

208   The chemical diffusion and reactions of elements are described by transport equations

209 including an advective term to account for the movement of the phase and conservation of

210 mass, a diffusion term (Fick's law) to account for diffusive transfer, and a reaction term

211 to account for the chemical transfer based on the partition coefficient between metal and

212 silicate. In our models we solve the following equation:

213
$$\frac{\partial c_i}{dt} + \nabla \cdot (-k_c \nabla c_i) + \boldsymbol{u} \cdot \nabla c_i = R_i \qquad (4)$$

214   Eq. 4 is the transport equation for diluted species including Fick's law for the diffusion of

215   an element $\left(\nabla \cdot (-k_c \nabla c_i)\right)$ with the addition of an advective term $(\boldsymbol{u} \cdot \nabla c_i)$ to account for

216 motions within the fluids. c_i is the concentration of element i in the phase of interest, k_c the

217 diffusion coefficient and R_i the reaction rate for element i.

218 In our case, there are no external sources of elements ($N_i=0$, Fig. 2).

219

220 We assumed the diffusion coefficient (k_c) to be the same for both phases, and independent

221 of the partition coefficient (D_i). Therefore we defined two functions to describe the

222 behavior of element i in each phase. One function (X_i^{sil}) describes the behavior of element

223 i in the silicate, and therefore tends toward 0 when $\Phi = 1$, the other (X_i^{met}) described the

224 behavior of element i in the metal and tends toward 0 when $\Phi = 0$. The combination of the

225 two functions give us the global concentration of element i in our computational domain.

226 The link between the two functions, the partitioning coefficient and the phase field is made

227 by defining a reaction at the interface between the metal and silicate (i.e. when $\Phi = 0.5$):

228 R_i is the reaction rate necessary to reach the chemical equilibrium defined by the metal-

229 silicate partition coefficient of element i (D_i). D_i is the Nernst partition coefficient given

230 by $D_i = \frac{X_i^{met}}{X_i^{sil}}$, where X_i^{met} is the mass fraction of element i in the metallic phase, and X_i^{sil}

231 the mass fraction of the same element in the silicate phase at equilibrium. R_i is given by

232 Eq. 5:

233
$$\frac{dc_i}{dt} = R_i \qquad (5)$$

234 Where c_i is the concentration in either silicate or metal in mol.m^{-3}, obtained from the

235 density of the phase where the element is ρ^{phase} (for either a metal or silicate phase), the

236   molar mass of the element (M_i) and the mass fraction of the element i in the phase

237   considered is represented by $c_i = X_i^{phase} \rho^{phase} / M_i$. R_i is automatically calculated in a

238   stationary state from the initial conditions and a given partition coefficient so as to reach

239   equilibrium using COMSOL's in-built solver before the simulation. The reaction rate is

240   high enough to maintain the equilibrium between two calculation steps: the typical time

241   for equilibration is 10^{-5} s, which is less than the time step solved by solver. R_i is negative

242   when removing siderophile elements from the metallic phase, and positive when creating

243   the same element in the silicate phase. The reaction function is only defined for the

244   metal/silicate boundary, given by the condition $\Phi = 0.5$. The higher the value of $D_i^{met/sil}$,

245   the closer the conditions are to equilibrium, and the lower the reaction rate (R_i) will be.

246   For the domain where $\Phi = 0$ or 1, the equilibrium is set to 0, and therefore the reaction

247   rate is 0. For a given time step, the in-built COMSOL Multiphysics 5.0 solver calculate

248   the Navier-Stokes equations (Eqs. 1 and 2) using finite element method, yielding the

249   velocity field. Then the level-set equation is computed at the same time the advection-

250   diffusion (Eq. 4) equation is solved by finite-element methods on the entire computational

251   domain, with the reaction R_i only defined where $\Phi = 0.5$.   The results of the calculation

252   are then used as starting condition for the next time step.

253

254 **2.3.** *Geometry, mesh and initial conditions*

255   First, we defined a geometry for the simulation, using one of the defined boundaries

256   for the eulerian solver available with COMSOL Multiphysics 5.0 software geometries.

257   The best choice for our type of simulation would have been be a 3-D model with a falling

258   sphere inside it, so as to compare our simulation to analog simulations (Deguen et al.,

259   2011, 2014; Wacheul et al., 2014). Since this type of simulation is very costly in terms of

260   computational time, especially for fluid flow simulations, we used a 2D-axisymetric

261   geometry, which solves the equation on a 2D surface, and uses the symmetry conditions

262   to give a 3D output. This is a good compromise between a 2D and 3D simulation when

263   the diapir is not fragmented. Our simulations focused on a weakly deformable falling

264   sphere (i.e. no break up) with a radius of 1 cm in a cylinder whose diameter was set during

265   the calibration of the simulation.

266

267   The geometry and boundary conditions used in this study are presented in Fig. 2. In

268   this geometry, a rotational symmetry axis is defined. For the fluid flow, the boundaries of

269   our calculation domain are characterized as follows:

270   -   on the top boundary, the condition is given by P= 1 atm,

271   -   on the bottom boundary, the condition is set to be a null velocity field

272   -   on the side boundary, the condition is a no slip condition

273   -   on all the boundary there is a no flow condition for the level set equation.

274   The conditions for chemical diffusion is a constant budget in chemical elements

275   throughout the numerical simulation, i.e. no elemental flux ($N_i = 0$), inward or outward, is

276   allowed on all the external boundaries.

277   For our calculation domain we used a fixed mesh of triangles, with three main

278   parameters: h_{max}, h_{min} and a curving parameter. The h_{max} parameter gives the maximum

279   size of the triangle side, h_{min} gives the minimum size and the curving parameter gives the

280   arc interception for curving triangles at spherical boundaries. The parameter controlling

281   the accuracy and the computation time for the calculation is h_{max}. The best value for this

282   parameter was determined in the resolution study, see Section 2.4.

283   The initial conditions are described in Fig. 2. The viscosities were varied for each

284   simulation, but the geometry of the set-up, the initial concentrations, the densities and the

285   droplet radius were kept constant. To avoid numerical instabilities inherent in $X_{sil}^0 = 0$

286   %wt , the initial concentration was set to $X_{sil}^0 = 10^{-4}$ %wt for the silicate with a density ρ_{sil}

287   = 3300 kg.m^{-3}; and $X_{met}^0 = 20$ % wt for the metal with a density $\rho_{met} = 8000$ kg.m^{-3}. The

288   radius of the droplet was $R_{Fe} = 1$cm, falling in a cylinder with a 5 cm radius and a 28 cm

289   height, with the center of the droplet placed initially at 26 cm height.

290

291 **2.4. Tests of the COMSOL simulation**

292   To correctly set up the computational domain in terms of size and mesh, two effects

293   need to be accounted for:

294   (1) Grid resolution, which has to be sufficient to capture the physics of small droplet

295   deformation.

296   (2) Boundary effects, to avoid a major influence of the outer border of the domain on

297   the flow and the generation of artifacts in the velocity field.

298   To minimize the numerical diffusion of iron during the diapir's descent, we tested several

299   maximum sizes for the mesh grid component h_{max}. Fig. 3 illustrates the time evolution of

300   the ratio between the calculated volume over the theoretical volume of one droplet (given

301   by $V_{theoretical} = \frac{4}{3}\pi R_{Fe}^{3}$ with R_{Fe}=1cm) for h_{max} values ranging between 0.06 and 0.2 cm.

302   The simulations were performed using the same initial geometry as in Fig. 2, with a silicate

303   and a metal viscosity of 100 Pa.s (corresponding to a Reynolds number of ~2. 10^{-3}, see

304   Eq. 6) and no chemical component to solve. The precision of the calculation increased as

305   the mesh size decreased, especially when there was deformation. On the other hand, the

306   smaller the mesh grid components were, the longer it took to complete the calculation. As

307   can be seen in Fig. 3, the precision is better for a mesh component size of 0.1 cm than for

308   smaller (0.06 and 0.08 cm) or larger (0.2 cm) mesh component sizes. In addition, a

309   maximum component size allowed a calculation time of a few hours (~ 6 hours), whereas

310   a mesh grid size of 0.06 cm yielded calculation times from a dozen hours to 2 days for the

311   less viscous flows. Therefore, for the rest of the study, we used a maximum size of 0.1 cm

312   for the mesh grid (i.e. $R_{Fe}/10$). The mesh size could be adapted to the type of flow for each

313   simulation: for example, for a higher degree of diapir deformation during the simulation

314   (typically for less viscous flows), the mesh size had to be decreased to avoid numerical

315   artifacts. To increase the precision, COMSOL also made it possible to set a minimum size

316   for the mesh grid component so as to get an adapted mesh, with smaller elements at the

317   interfaces between the two phases, and larger elements as the distance from the interface

318   increases. Varying the parameter h_{min} did not affect the simulation for a given value of

319   h_{max}, so it was kept at a constant value of $h_{min} = h_{max}/40$.

320

321   The second point was to avoid boundary effects on the fluid flow during the simulation.

322   We tested several domain sizes and checked the different velocity field components (r-

323   and z- components). We chose a height equal to $28xR_{Fe}$ and a width equal to $5xR_{Fe}$ which

324   was sufficient to avoid the recirculating flow associated to the descending diapir having a

325   large effect on the velocity field (Fig. 4), while keeping computational time within

326   reasonable bounds. This size of domain still affected the velocity of the diapir (Chang,

327   1961 and Fig. 4). Fig. 4 shows that increasing the width to 6x R_{Fe} changed the velocity

328   field, albeit very slightly, which indicates a diminution of the wall effect: the mean

329   velocity of the diapir increased by 8 % compared to the mean velocity for a width of $5xR_{Fe}$.

330   However, increasing the width of the domain from 5xR_{Fe} to 6xR_{Fe} led to a significant

331   increase in computational time (by at least 46 %). Given the limited effect of increasing

332   the domain width and the significant effects on the computational time, we considered this

333   smaller width to be suitable for the study. We applied the same reasoning to choose the

334   height of our domain. To test the resolution of the diffusion in Eq. 4, we benchmarked the

335   validity of the COMSOL solver against steady and unsteady analytical solutions for

336   diffusion problems (Crank, 1975). To test the advective part, we compared the flow

337   velocities from our models with those velocities obtained by Samuel (2012) (see section

338   3.2). Our results showed an acceptable agreement, despite a large discrepancy between

339   theoretical results and observed velocities (45% for the largest one) for flows with the

340   largest velocities, i.e. in the intermediate regime. To explain the observed differences, we

341   calculated the mesh Peclet number Pe_{mesh} after each simulation with $Pe_{mesh} = \frac{vh_{max}}{k_c}$,

342   where v is the velocity of the diapir, h_{max} is the mesh size and k_c is the diffusion coefficient

343   (10^{-6} m^2.s^{-1}, which is higher than a typical chemical diffusion, but high enough to limit

344   numerical diffusion (see Qaddah et al., 2020). In the reference case and for the other cases

345   within the Stokes regime, the value of Pe_{mesh} was sufficiently low ($Pe_{mesh} < 10$) meaning

346   that numerical diffusion was negligible (see Mittal & Jain, 2012). For the cases within the

347   intermediate regime, Pe_{mesh} was higher ($Pe_{mesh} > 50$), which indicates possible numerical

348   diffusion that likely affected our results. To correct this effect a much smaller mesh size

349   would have been necessary. However, the mesh size necessary to prevent numerical

350   diffusion in our models would have led to unreasonable computational times. Therefore,

351   for the lowest viscosity used in our models some error calculations might have occurred

352   in our results, but are negligible in the final model (see Section 5 and 6).

353

354   **3. Results**

355   In this section we present the results of our simulations as well as a definition of the non-

356   dimensional numbers and parameters used to interpret the results of the simulation in

357   terms of degree of equilibrium. A reference run was arbitrarily defined to set a reference

358   time evolution for the non-dimensional parameters. Then we varied the viscosity of the

359   silicate and metallic phase for a given partition coefficient value, and finally we varied the

360   value of the partition coefficient for a given viscosity.

361

362   **3.1. Reference case and characteristic non-dimensional numbers**

363   In this section we present the results for a reference case, where $\mu_{sil} = \mu_{met} = 100$ Pa.s.

364   The temporal evolution of the reference case flow is presented in Fig. 5. This figure shows

365   that for this case both the diapir deformation and the numerical diffusion are weak. The

366   metallic droplet moves a distance of $10 \times R_{Fe}$ (10 cm) in 12.1 seconds.

367

368

369   To compare this flow to other flows with different viscosities, we need to use non-

370   dimensional numbers. Since this study focuses on the viscosity variations and the

371   characteristics of the flow, the Reynolds number (*Re*) is the more adequate non-

372   dimensional number, which is given by Eq. 6:

373

374                          $$Re = \frac{\rho_{sil} R_{Fe} v_{diapir}}{\mu_{sil}}$$ (6)

375   where ρ_{sil} is the density of the surrounding silicate, R_{Fe} is the initial radius of the diapir,

376   v_{diapir} is the velocity of the diapir and μ_{sil} is the silicate viscosity (see Table 1). This number

377   expresses the ratio of inertial forces to viscous forces. When *Re* < 1, the flow is considered

378   to be a Stokes flow, which means that diapir deformation is limited during the descent.

379   When 1<*Re*<500, the flow is an intermediate flow between Newtonian and Stokes flow

380   (Samuel, 2012). In our study, we did not investigate the case of *Re* > 500, which is a highly

381   turbulent Newtonian flow.

382

383   The velocity of the diapir is strongly governed by the viscosity of the surrounding silicate,

384   which affects the value of *Re* (*e.g.* Samuel, 2012, and references therein). In order to

385   compare different values of the viscosity ratio $R_\mu = \mu_{met} / \mu_{sil}$, we defined the reference

386   time for each calculation as the time necessary for a metallic droplet with radius R_{Fe} to

387   move through a distance $d=10 \times R_{Fe}$.

388   The other non-dimensional number which controls the flow is the Weber number

389 (*We*), which is the ratio of the inertial forces on the surface tension:

390 $$We = \frac{\rho_{sil} v_{diapir}^2 R_{Fe}}{\sigma} \qquad (7)$$

391   with σ the surface tension (see Tab. 1 for value). The break-up of the diapir is controlled

392 by the Weber number (Wacheul et al., 2014). When $We < 6$ the diapir is stable in Stokes

393 and intermediate flows, and when $We > 6$ the surface tension is no longer high enough to

394 prevent the diapir breaking up (Wacheul and Le Bars, 2017). In this case and in the rest of

395 the present study, the diapirs are always stable with $We < 6$. For the reference case, the

396 diapir velocity is about $v_{diapir} \approx 8 \times 10^{-3}$ m.s^{-1}. This velocity yields low values of *Re* and *We*

397 (2.2×10^{-3} and 1.2×10^{-3}, respectively), which explains the diapir's stability during its

398 descent (see Fig. 5).

399

400 To study the chemical equilibrium between metal and silicate, we calculated a non-

401 dimensional concentration, or more precisely a non-dimensional mass fraction termed *X'*.

402 This non dimensional mass fraction was calculated so as to satisfy three conditions:

403   (i)   If there is no change in the initial concentration in the silicate, *X'* is equal to 0

404   (no equilibrium at all)

405   (ii)   If equilibrium is reached, *X'* is equal to 1.

406   (iii) X' is proportional to the concentration in the silicate $(X' \propto X)$

407   The first condition is reached if $X = X_{sil}^0$. Therefore $X' = 0$ implies a null numerator for

408   X', i.e. $X' \propto X - X_{sil}^0$. For the second condition, it is reached if $X = X_{met}^{eq}\big/D^{met/sil}$, by

409   definition of the partition coefficient, where X_{met}^{eq} is the concentration of the element in

410   the metallic phase at equilibrium. In our case, the element is a siderophile ($D^{met/sil} \geq 1$)

411   and the initial concentration is high ($X_{met}^0 = 0.2$). Therefore, at the end of the simulation

412   we could approximate the equilibrium concentration by $X_{met}^{eq} \sim X_{met}^0$. Satisfying the

413   condition $X' = 1$, with $X' \propto X - X_{sil}^0$ and the non-dimensionality of X' yield to the

414   following formula given in Eq. 8:

415
$$X' = \frac{X - X_{sil}^0}{X_{met}^0/D^{met/sil} - X_{sil}^0} \tag{8}$$

416   X' is a useful parameter for tracking the evolution of concentration in a particular case,

417   but it is not enough to quantify how much of the silicate is affected by a change in

418   concentration. Moreover, this parameter is not suitable for comparing different studies,

419   because it is strongly affected by the duration of the sinking. The evolution of the non-

420   dimensional concentration, X', in the reference case is shown in Fig. 6. Equilibrium in the

421   silicate is reached when $X' = 1$ (area in red). This area forms a very narrow zone around

422   the diapir, and most of the silicate is not chemically equilibrated with the metal, because

423   the simulation run time is not long enough.

424   The parameter R_C is the ratio of the silicate volume that has reacted with the metal to the

425   total volume of silicate. The definition is $R_c = V_{reacted}^{sil}/V_{total}^{sil}$, where $V_{reacted}^{sil}$ is the

22

426   volume of silicate where $X > X_{sil}^0$; meaning R_C is the volume fraction of silicate that has

427   reacted with the metal. To visualize how the ratio is calculated, a representation of the

428   integrated volume is shown in Fig. 7. In this figure, the areas colored in red represent the

429   volume of silicate that has evolved in terms of chemical composition, while the areas in

430   blue represent that which has not been contaminated by the diapir's descent.

431   For each simulation, the volume chemically affected by the diapir's descent increases with

432   time. The time evolution of the R_C value for the reference case is shown in Fig. 8. R_C is

433   increasing with time following the same trend in each case. The difference is in the

434   absolute values of $D^{met/sil}$: the more elevated the value is, the closer the initial conditions

435   are to equilibrium conditions, which leads to a lower reaction rate.

436

437

438   **3.2. Range of *Re* and *We* values**

439   The aim of our models was to constrain the influence of the viscosity contrast between

440   the silicate and metallic phases. This led to a wide range of *Re* and *We* values in our

441   numerical simulations. The viscosity of the silicates surrounding the metal droplet controls

442   the flow regime and the sinking velocity. The evolution of the time necessary to reach the

443   distance of $10 \times R_{Fe}$, which depends mostly on the silicate viscosity (Samuel, 2012 and

444   references therein), is presented in Fig. 9. The higher the viscosity of the silicate, the longer

445   it takes for the diapir to reach a set distance. The changes in flow regime result in different

446   expressions for the diapir velocity. In our study, the range of *Re* values only allows Stokes

447   regime flows (*Re* < 1) or intermediate regime flows (1<*Re*<500), with two different

448   expressions for the diapir's velocity. In a Stokes flow the velocity is given by:

449    $$v_{Stokes} = \frac{2}{9} \frac{(\rho_{met} - \rho_{sil})gR_{Fe}^2}{\mu_{sil}} \tag{9}$$

450   For intermediate flows, the sinking velocity is given by:

451    $$v_{intermediate} = 2\sqrt{\frac{(\rho_{met} - \rho_{sil})gR_{Fe}}{\rho_{sil}C_D}} \tag{10}$$

452   with C_D the drag coefficient. In our case, the drag coefficient is approximated by $C_D =$

453    $\frac{12}{Re} + 0.3$, following Samuel (2012). From Eq. 10, we can also calculate the velocity in

454   each drop flow regime: Stokes, intermediate, and Newton (e.g. Qaddah et al., 2019). The

455   theoretical times associated with the velocity are compared to the actual times observed in

456   simulations in Fig. 9. It shows a good agreement between theoretical and observed diapir

457   velocity, despite some scatter. This scatter is consistent with the wall effect of our

458   simulations: the variation in velocity observed in the Stokes flow is of the order of 10 %,

459   which is consistent with the variation expected if the wall effect is negligible (see Section

460   2.4). Comparison with the typical equilibrium time from Wacheul et al. (2014) in Fig. 9

461   shows that, except for the intermediate flows, the fall time chosen in our study is long

462   enough to reach full equilibrium (or more than 90 % of equilibrium in some cases) inside

463   the metal, leaving the silicate as the limiting phase for equilibrium. The dispersion of the

464   obtained reference time (Eqs. 8 and 9) in Fig. 9 for a chosen value of μ_{sil} is considered

465   therefore as a negligible discrepancy in the rest of the study.

466   In Fig. 10 we plot the *Re* values as a function of the *We* values for each simulation (i.e.

467   for each viscosity contrast used in our calculations). The velocity of the diapir (v_{diapir}) used

468   to calculate *Re* and *We* is determined from our numerical models by the time necessary for

469   the diapir to move through a distance of $10\times R_{Fe}$. This time is dependent on the viscosity

470   and illustrated in Fig. 9. Fig. 10 (left) shows that in all our numerical simulations, the

471   metallic droplet is stable (i.e. no break up occurs) even though some models are in the

472   Stokes regime and others are in the Intermediate flow regime. In Fig. 10 (right) we

473   compare the range of values with the range of *We* and *Re* values relevant to the geological

474   context of a liquid metallic droplet sinking through a terrestrial magma ocean (Wacheul et

475   al., 2014). As shown in Fig. 10 (right), our range of values is limited compared to possible

476   geophysical values. Larger diapirs leading to high *Re* and *We* values are not considered in

477   our study, which focuses on small droplets in the iron rain scenario.

478

3.3. Influence of the viscosity ratio

480   The viscosity ratio is an important parameter controlling the dynamics of diapir

481   descent, both its shape (Qaddah et al., 2019) and stability (Wacheul et al., 2014). In this

482   section, we focus on the influence of the viscosity ratio R_μ $(=\mu_{met}/\mu_{sil})$ by varying the value

483   of the silicate viscosity for a given metal viscosity. Changing the viscosity of metal affects

484   its ability to deform and, hence, its terminal velocity, but this effect is not as strong as the

485   change in velocity implied by a change in ambient viscosity. This behavior is consistent

486   with the equation of diapir velocity in Stokes and intermediate flows (Eqs. (9) and (10)),

487   and is strongly dependent on the silicate viscosity. It is visible in Fig. 9, where a decrease

488   in silicate viscosity from 1000 Pa.s to 10 Pa.s (Stokes flows) leads to an increase in sinking

489   velocity from 10^{-3} m.s^{-1} to 0.1 m.s^{-1} for a metal viscosity of 1 Pa.s. For a constant silicate

490   viscosity of 10 Pa.s, a decrease of the metallic viscosity from 1000 Pa.s to 0.1 Pa.s only

491   increases the velocity from 0.05 to 0.1 m.s^{-1}. The viscosity ratio influences the sinking

492   velocity and, hence, affects the Re number and the flow regime, but not as strongly as the

493   silicate viscosity.

494   Fig. 11 illustrates the influence of the Re number on the silicate volume chemically

495   contaminated during the sinking of a metallic droplet with R_{Fe}=1cm. For each case, the

496   evolution of R_C is shown as a function of Re, and for a distance of 10 cm (10×R_{Fe}). The

497   time corresponding to this distance is shown in Fig. 5 as a function of viscosity. Except

498   for the case with $D^{met/sil} = 10^3$, there is no linear correlation between $\log(R_C)$ and $\log(Re)$.

499   However, we clearly show a transition between the Stokes regime and the Intermediate

500   regime. In the Stokes regime flow, an increasing Re (i.e. a decreasing value of μ_{sil}) leads

501   to a significant decrease of R_C, while R_C values seem to reach a plateau when the flow

502   reaches the intermediate flow regime. Fig. 11 also shows that the approximation made by

503   Rubie et al. (2003) to achieve an analytical solution for equilibrium is only valid for low

504   *Re* flows (high silicate viscosity). As the density of the silicate is not significantly altered

505   by the reaction, the parameter R_c (volume ratio of silicate equilibrated) can be compared

506   to their parameter F_s (mass ratio of silicate equilibrated). For the lowest *Re* value, there is

507   good agreement between our numerical data and the analytical calculation. However,

508   extrapolating the analytical solution to higher *Re* flows leads to an overestimation of the

509   equilibrated volume.

510   The R_C ratio is presented in Fig. 12 as a function of R_μ. A decrease in R_C is observed with

511   an increase in R_μ (i.e. a decrease of μ_{sil}) for a given viscosity of the metallic phase. For the

512   five parts of Fig. 12, which correspond to the five values of μ_{met}, the trend and the

513   magnitude of the values of R_c are quite similar, meaning that the effect of the viscosity

514   ratio is less important than the ambient viscosity, which governs the flow regime. For high

515   values of R_μ, the same plateau phenomenon as seen in Fig. 11 is observed, which

516   corresponds to lower silicate viscosity values (intermediate flow). In the Stokes regime,

517   the sinking velocity scales with μ_{sil}^{-1} (Eq. (9)) while in the intermediate regime, the sinking

518   velocity scales with C_D^{-1}. Given the expression of the drag coefficient (derived from

519   Samuel, 2012; see Section 3.2), and the expression of *Re* (Eq. (6)), the sinking velocity in

520   the intermediate regime scales with $(\rho_{sil}\mu_{sil})^{-0.5}$, as given by Eq. (10). Hence, R_μ has a

521   greater effect on Stokes flows than intermediate flows, because the changes in diapir

522   velocity are more pronounced for Stokes flows, as shown in Fig. 5.

523   Although the evolutions of R_C as a function of R_μ are quite similar in the five panels of

524   Fig. 12, some differences are noticeable. For the lowest values of $\mu_{met,}$ the R_C ratio

525   increases at high R_μ values while for high values of $\mu_{met,}$ the R_C ratio is nearly constant or

526   decreases with high R_μ (except for $D^{met/sil} = 1000$). This could be explained by the fact that

527   a higher viscosity ratio tends to stabilize the diapir and slow down its descent (Wacheul

528   et al., 2014). In a Stokes regime, it leads to an increase in the time necessary to reach the

529   same distance, in other words a longer reaction time; but in intermediate regimes this time

530   does not change significantly, while the diapir is less deformed, leading to a smaller

531   surface of exchange between metal and silicate. We illustrate this point in Fig. 13, for a

532   silicate viscosity of 0.1 Pa.s: the normalized surface of the diapir varies from 1 to 2.3 with

533   decreasing values of R_μ, which means that low R_μ for high Re (~100) values lead to an

534   increase of exchange surface by 130% relatively to the initial diapir surface. The same

535   effect is observed for $\mu_{sil} = 1$ Pa.s (Re~10), to a lesser degree: for low metallic viscosity

536   ($R_\mu = 0.1$) the diapir surface increases by 20%. This leads to an increase in R_c value for all

537   partition coefficients except for $D^{met/sil} = 1000$, for which an increase in diapir surface has

538   a negligible effect, the deformation occurring over a short timescale at a low reaction rate.

539   This effect is weak in our study compared to the effect of Re and $D^{met/sil}$ (see Section 3.4),

540   because the We range of our study does not allow major diapir deformation. For the

541   deformation rate to have a strong impact on chemical equilibrium, the We values have to

542   be much higher ($We > 10$, see Lherm & Deguen, 2018).

543

544

3.4. Influence of the partition coefficient

We have shown in Figs. 11 and 12 that chemical equilibration was less efficient when the value of the viscosity ratio between the iron and silicate phases was higher. This conclusion also stands for the whole range of partition coefficients used in our models. As detailed in Section 2.2, the higher the value of $D^{met/sil}$, the closer the conditions are to equilibrium conditions, and the lower the reaction rate (R_i) will be. However, the thermodynamical equilibrium is reached faster, which limits the amount of exchange between the metallic droplet and the surrounding silicate. Therefore, the contaminated volume represented by R_C decreases when $D^{met/sil}$ increases (see Figs. 11 and 12). This effect is relatively small: an increase of 3 orders of magnitude decreases Rc by less than one order of magnitude.

3.5. Parameterization of the chemical contamination

As shown in the previous sections, the contamination of silicate by a siderophile element depends on the Reynolds number, viscosity ratio, and the values of metal-silicate partition coefficients. To use our results in an iron rain scenario following an impact during planetary formation, it is necessary to quantify the relative effect of each parameter on chemical contamination. In section 3.1 and 3.2 we chose a distance of $10 \times R_{Fe}$ and the relevant time (Fig. 5) at which R_C is considered to have reached a stationary value. With

29

565   this assumption the error is limited, since R_C tends to reach a plateau in all our simulations

566   (see Fig. 8). Therefore, we consider the R_C values obtained from our models at a distance

567   of $10 \times R_{Fe}$ in our parameterization.

568   We show in Sections 3.2 and 3.3 that increasing the Reynolds number and viscosity

569   ratio both tend to decrease R_C. In Figs. 11 and 12, $\log(R_c)$ decreases linearly with both

570    $\log(Re)$ and $\log(R_\mu)$ independently of the value of $D^{met/sil}$ with a small error in the prediction

571   ($R^2 > 0.85 - 0.9$). Concerning the effect of partition coefficients, (Section 3.4), all the

572   curves in Figs. 11 and 12 are parallel, showing that there is a linear relationship between

573    $\log(R_c)$ and $\log(D^{met/sil})$. We parameterize the evolution of $\log(R_C)$ as a function of $logRe$,

574    $logR_\mu$ and $logD^{met/sil}$. The method used here is a multi-linear regression fit on all the data

575   retrieved from the simulations:

576    $$logR_C = a \times logD^{met/sil} + b \times logRe + c \times logR_\mu + d \tag{11}$$

577

578   where a, b, c and d are constants fitted to the data by least-square regressions. The values

579   of the parameters are presented in Table 2. As shown in Fig. 14, the parameterization of

580   Eq. (11) shows a relatively good fit to the data retrieved from calculations. This kind of fit

581   is not perfect, and could certainly be improved by including non-linear dependencies. It is

582   also worth noting that this parameterization is valid for a narrow range of Re and We

583   values, and its precision is lower at high Re values (see section 2.4). For instance, different

584   results can be found in turbulent cases (high Re, Deguen et al., 2014) and/or with deformed

585 diapirs (high *We*, Lherm & Deguen, 2018). However, this form of equation (Eq. (11)) is

586 practical to use in models of planetary formation with limited error on the value of R_C,

587 therefore we chose this form to simplify the calculations in sections 5 and 6.

588 This parameterization shows that the main parameters controlling the

589 contamination of a liquid silicate reservoir by a siderophile element during the sinking of

590 a metallic droplet are the Reynolds number and the metal-silicate partition coefficients.

591 The higher the $D^{met/sil}$ is, the less the silicate will be contaminated, which reflects the fact

592 that we consider here a siderophile element. The Reynolds number has the same effect as

593 $D^{met/sil}$: the higher *Re* is, the lower R_C will be. This high absolute value of *b* reflects the

594 importance of the silicate viscosity, which controls the diapir velocity, as well as the type

595 of flow and the deformation of the diapir. The fact that the parameter *b* is negative shows

596 that increasing the value of the Reynolds number will decrease R_C. Indeed, decreasing the

597 viscosity increases the Reynolds number (Eq. 6) as well as the diapir velocity (*e.g.* Samuel,

598 2012; Wacheul et al., 2014, and Fig. 5).

599

4. From a single droplet to the large impact context

601 In the previous section, we derived a parameterization (Eq. 11) to estimate the volume

602 fraction of a magma ocean contaminated by a unique 1cm-radius metallic droplet. In this

603 section we apply this parameterization to large impacts in the context of late accretion.

604 The parameterization was calculated for a pertinent range of metallic and silicate

605 viscosities. Numerical simulations and laboratory experiments estimated the viscosity of

606 silicate melts at high pressure within the range of 0.01 Pa.s to 1 Pa.s. (Liebske et al., 2005;

607 Karki & Stixrude, 2010; Karki, 2018). This range is stable because the viscosity tends to

608 increase with pressure, but decrease with increasing temperature. As for the viscosity of

609 metallic liquid, few experiments have been made, but the experimental results also show

610 that the range of viscosity for liquid iron alloy is stable, at around 0.01-0.1 Pa.s (Kono et

611 al., 2015). Therefore, the effect of viscosity on the equilibrium rate calculated in our

612 simulation can be extrapolated for a high pressure context in an entirely liquid magma

613 ocean. The higher values (10 -1000 Pa.s) of μ_{sil} tested in our simulation can also be applied

614 at the end of the magma ocean stage when the silicate liquid is starting to crystallize (but

615 before the mushy stage where the flow dynamics is governed by the viscosity of the solid

616 silicate phase).

617 A more limiting factor to the extrapolation of our parameterization to planetary formation

618 is the size of our computational domain. However, it is possible under certain conditions,

619 which are listed below.

620 When a differentiated impactor collides with a growing planet, two fragmentation

621 mechanisms of its metallic core occur. The first fragmentation is induced by the impact

622 itself that stretches and disperses the impactor's core (Kendall and Melosh, 2016). The

623 lunar crater observations showed that the most probable impact angle is $\alpha = 45°$

624   (Shoemaker, 1962). When considering an impactor with a metallic core radius of R_{core}

625   impacting a magma ocean at an angle α = 45°, it is possible to apply our parameterization:

626   the dispersion of the impactor's core material becomes the same as our study

627   computational domain. The mantle fraction affected by the impact (i.e. the volume of

628   mantle into which the metallic droplets are initially spread out) can be approximated by

629   the volume of a cylindrical portion with an angle α, a thickness h and a radius L. The

630   volume of mantle affected is then $V_{affected} = \alpha h L^2 / 2$. For R_{imp}=100 km, R_{core}=50 km,

631   and α=π/4, Kendall & Melosh (2016) give h=200km, L=2000 km: we can then estimate

632    $V_{affected} = 3.14 \times 10^{17}$ m^3. After the first fragmentation induced by the impact, a second

633   rapid fragmentation occurs leading to the formation of much smaller droplets of different

634   sizes. Wacheul et al., (2014) showed that metallic diapirs will fragment into droplets with

635   a mean radius of between 4 mm and 20 mm. Assuming an average droplet radius of 1 cm

636   (Rubie et al., 2003) and that all the impactor's core diapir is fragmented into these cm-

637   radius droplets, an impactor's core with radius R_{core}=50 km will fragment into ≈10^{20} cm-

638   radius droplets. This yields a concentration of 400 droplets/m^3, or 1 droplet per 2.5 liters,

639   which yields a metal/silicate volume ratio of 0.0016 within $V_{affected}$. Currently, no scaling

640   law describes the relation between (L, h, α) and R_{imp} (and as a consequence R_{core}).

641   According to Kendall & Melosh (2016), for R_{core}=50km, L≈40R$_{core}$ and h ≈ 4R$_{core}$ and by

642   making the assumption that these two relations are also valid for different R_{core} values, we

643 can infer that the ratio of the impactor's core volume over the affected volume is constant

644 for any impactor size.

645

646 In the numerical models described in the previous sections, we consider a metallic droplet

647 sinking into a large volume of molten silicates to avoid boundary effects. In our study the

648 ratio between the volume of the iron droplet and the volume of the computational domain

649 is 0.0019, which is relatively close to the volume ratio of 0.0016 expected after an impact.

650

651 After a large impact, the impactor's core is dispersed within a volume $V_{affected} =$

652 $\alpha h L^2/2$. Assuming the formation of a cloud of cm-radius droplets with an iron fraction

653 $\chi_{Fe} = 0.0016$ within $V_{affected}$, the volume where chemical exchange between the

654 droplets and the magma ocean will occur is:

655

656 $$V_{exch} = R_c V_{affected} \qquad\qquad (12)$$

657

658 Using Eq. (11), Tab. 2 and considering $L=40R_{core}$ and $h = 4R_{core}$ (Kendall and Melosh,

659 2016), we can calculate the fraction of the volume of the Earth's mantle V_{exch}/V_{mantle} in

660 which chemical exchange is likely to occur. Fig. 15 shows V_{exch}/V_{mantle} as a function of the

661 impactor radius and illustrates the influence of the partition coefficient and the viscosity

662 contrast between the magma ocean and the liquid iron on this ratio.

663

As the impactor size increases, the mantle volume chemically affected by the impact

increases by R_{imp}^3. This relation is constrained by the simple formula we have used to

relate $V_{affected}$ to R_{core}. Given the current knowledge of the impact-induced fragmentation

mechanisms of an iron core on a planetary scale, this simplification is a first step toward

a global understanding of the chemical equilibration occurring after a large impact. Fig.

15 (left) illustrates that an increase in partition coefficient leads to a decrease in the ratio

V_{exch}/V_{mantle} in agreement with Eq. (11) and the values from Tab. 2. Fig. 15 (left) shows

that for R_{core}=1000 km, increasing the partition coefficient by 2 orders of magnitude

decreases the value of the ratio V_{exch}/V_{mantle} by a factor of 3. This effect is significant but

less important than the influence of the viscosity ratio. Fig. 15 (right) shows that

increasing the magma ocean viscosity relative to a constant liquid iron viscosity of 0.1

Pa.s from 0.1 Pa.s to 100 Pa.s leads to an increase in V_{exch}/V_{mantle} by a factor of more than

5. According to Fig. 15, a very large impact such as that which led to the formation of the

Moon-Earth system, involving a highly viscous magma ocean, would strongly enhance

the chemical equilibration between the impactor's core and the Earth's mantle. This result

needs to be nuanced, since a large impact is likely to increase temperature and therefore

lower the viscosity of the magma ocean.

681

5. Signature of a large impact on the mantle composition

This section aims at improving previous accretion models (e.g. Fischer et al., 2015, Siebert et al., 2012, Wood et al., 2008) by accounting for a possible chemical disequilibrium at a given depth. Previous models assumed that at a given step in accretion, equilibrium is reached throughout the entire mantle (Wood et al., 2008; Siebert et al., 2012; Boujibar et al., 2014; Clesi et al., 2016). This equilibrium is set by the final pressure on reaching equilibrium, usually at a depth corresponding to 50 % of the core mantle boundary depth (or close to this depth, for instance in Rubie et al., 2015), in order to fit the Ni and Co partitioning behavior (Bouhifd & Jephcoat, 2003;2011; Fischer et al., 2015).

In this section and the following one, the hypothesis is the same as in previous models of accretion, but with the notable exception that not all of the mantle reaches equilibrium. The amount of mantle equilibrated is defined using Eqs. (11) and (12), i.e. our parameterization is applied directly to a classical model of equilibration in a magma ocean, thus adding one step of complexity to previous models.

5.1.   Geochemical elements of interest

To estimate the chemical equilibrium between the impactor's core and the impacted mantle, we focus our calculations on the chemical behavior of moderately siderophile elements such as Ni and Co for which $D^{met/sil}$ is strongly dependent on pressure (Bouhifd & Jephcoat, 2003, 2011; Siebert et al., 2012; Fischer et al., 2015). These two elements are important, since the models of deep magma ocean are designed to explain their relatively high abundances in the BSE (Drake and Righter, 2002). The maximum depth of the
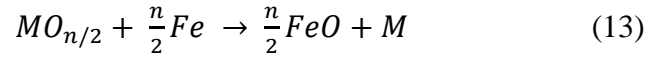
704   magma ocean (around 50% the CMB depth throughout accretion) is derived from the

705   pressure for which the partitioning behavior of Ni and Co yields a 19.05±2 ratio in the

706   BSE (Bouhifd & Jephcoat, 2003, 2011). In the previous sections, we considered a generic,

707   moderately siderophile element with a metal/silicate partition coefficient ranging from 1

708   to 1000. This range is large enough to extrapolate the trend derived from our simulations

709   to the behavior of Ni and Co at high pressure. For Ni, this partition coefficient ranges

710   between ≈400 for P =1 GPa, and ≈ 20 for 40<P<60 GPa. For Co, the partition coefficient

711   ranges between ≈ 100 for P = 1 GPa and ≈ 20, for 40<P<60 GPa (Bouhifd & Jephcoat,

712   2011 and references therein). In the models presented below, we assume that the pressure

713   of equilibrium after an impact corresponds to the last stages of equilibrium in a deep

714   magma ocean, at between 50 and 60 GPa (see Appendix B in Clesi et al., 2016 for the

715   corresponding calculations and the full evolution of pressure, temperature and f_{O2} during

716   the accretion) with values of Ni and Co partition coefficients of between 20 and 80 for the

717   corresponding f_{O2}. In the following section, we consider that the iron content of the mantle

718   is close to the BSE content (8% wt) and is not affected by the impact. The f_{O2} is then

719   considered constant relatively to the iron-wüstite buffer and its value is $\log f_{O2} \approx$ -2 ΔIW.

720   In this case, the Ni and Co partition coefficients have converged toward the same value:

721     $D^{met/sil} \approx 20$, which is used in the following calculations.

722

5.2.   Chemical signature of a large impact on the Ni/Co ratio

Here we characterize the effect of a single impactor on the Ni/Co ratio in the mantle. We consider an initially fully accreted Earth. The reference composition of the impacted mantle is set to the BSE composition defined in McDonough and Sun, (1995) (Ni/Co = 19.05, 2000 ppm of Ni and 105 ppm of Co in the mantle). We consider that the silicate fraction of the impactor is lost during impact and that only its metallic core is trapped within the impacted mantle. The impactor has a radius of between 10 km and 1000 km and the same composition as the Earth's core (McDonough, 2003). Given the range of impactor size, the mass accreted is negligible compared to the Earth's mass: with a mean density of 9400 kg.m^{-3}, a metallic impactor of 1000 km radius adds a total mass of $\sim 3.10^{22}$ kg, which is 0.5% of the Earth's mass. This choice of size and composition for the impactor allows us to focus on the change in mantle concentration, without changing the final core concentration, especially the light element (Si and S) content, in the core. Furthermore, this impactor composition, and its relatively low mass, would not significantly change the oxygen fugacity and thus does not affect the partitioning behavior of Ni and Co.

This section aims at characterizing the partitioning behavior of Ni and Co as a function of the impactor radius and the viscosity contrast R_μ computing Eqs. (11) and (12). The first term of Eq. (11) illustrates the influence of the partition coefficients for Ni and Co. These

743 partition coefficients are controlled mainly by pressure and temperature, as well as the

744 composition of the metallic phase, and oxygen fugacity (Bouhifd & Jephcoat, 2003, 2011,

745 Siebert et al., 2012, Fischer et al., 2015). To obtain partitioning behavior independent of

746 oxygen fugacity, we use the exchange partition coefficient K_d, which is the

747 thermodynamical constant of the reaction:

748 $$MO_{n/2} + \frac{n}{2}Fe \ \rightarrow \ \frac{n}{2}FeO + M \qquad\qquad (13)$$

749 Where M is the element considered (in our case Ni or Co), and n is the valence of the

750 element M (in our case, n= 2). In reaction (13), the oxides are in the silicate phase, while

751 the reduced element is in the metallic phase. The exchange partition coefficient is given

752 by $K_d = \frac{c_M}{c_{MO_{n/2}}} \times \left(\frac{c_{FeO}}{c_{Fe}}\right)^{n/2}$ where c_M and c_{Fe} are the molar fractions of M and Fe in the

753 metallic phase, and c_{FeO} and $c_{MO_{n/2}}$ are the molar fractions of FeO and $MO_{n/2}$ in the

754 silicate phase.   To estimate the values of the partition coefficients, we use the

755 parameterization of K_d from Clesi et al., (2016), where we ignore the effect of water, as

756 well as the carbon content in the metallic phase. The exchange partition coefficient, K_d, is

757 given by:

758

759 $$logK_d^{element} = \frac{b_{el}}{T} + c_{el}\frac{P}{T} + e_{el}log\left(1 - \chi_{Si}^{metal}\right) + g_{el}log\left(1 - \chi_S^{metal}\right) + h_{el}$$

760 (14)

761

762 The parameters b_{el}, c_{el}, e_{el}, g_{el} and h_{el} are detailed in Clesi et al., (2016), and are different

763 for each element studied. *P* and *T* are the pressure (in GPa) and temperature (in Kelvin)

764 of equilibrium, respectively, corresponding to the pressure at 50% of CMB depth (i.e.,

765 1450 km), and the liquidus temperature associated with it (Andrault et al., 2011). We

766 assume here an equilibrium pressure of 63 GPa, and an equilibrium temperature of 3450

767 K. χ_{Si}^{metal} and χ_{S}^{metal} are the mass fractions of silicon and sulfur in the impactor. We

768 assume here that $\chi_{Si}^{metal} = 0.06$ and $\chi_{S}^{metal} = 0.019$ (McDonough, 2003). K_d is then

769 converted into a Nernst partition coefficient (mass ratio) following:

770

771 $$D^{met/sil} = \frac{M_{oxide} \times M_{Fe}}{M_{FeO} \times M_{element}} \times K_d^{element} \times D_{Fe}^{met/sil} \qquad (15)$$

772

773 where $M_{element}$ is the molar mass of Ni or Co, M_{oxide} is the molar mass of NiO or CoO, and

774 M_{Fe} and M_{FeO} are the molar masses of Fe and FeO respectively. $D_{Fe}^{met/sil}$ is the partition

775 coefficient of iron and equals 13.65 in the BSE model. We consider that the impactor does

776 not significantly change the oxygen fugacity and therefore does not influence the $D_{Fe}^{met/sil}$

777 value.

778 The second term in Eq. (11) characterizes the influence of the Reynolds number, which is

779 given by Eq. (6). As stated in Section 4, we consider that the metal fragments into droplets

780 with a radius of 1 cm. The sinking velocity of these droplets is given by Eq. (9). We

781 assume here a silicate density of $\rho_{mantle} = 4500$ kg.m^{-3} (mean density of the Earth's mantle),

782   a metallic density of ρ_{metal}= 9400 kg.m^{-3}, which is consistent with iron rich liquid alloys

783   at these pressures (Morard et al., 2013) and the current Earth's value for the acceleration

784   of gravity (i.e., 9.81 m.s^{-2}). The viscosity of the silicate phase in our calculations ranges

785   from 0.1 to 100 Pa.s. The third term in Eq. (11) measures the influence of the viscosity

786   ratio $R_\mu = \mu_{met}/\mu_{sil}$. In our calculations, we consider a constant value for the metallic

787   viscosity (= 0.1 Pa.s), consistent with iron liquid viscosity at high pressure (Kono et al.,

788   2015).

789

790   Once the parameter Rc is calculated for Ni and Co, the impactor equilibrates with a volume

791   of mantle defined by Eq. (12) in section 4, considering that $V_{impactor}/V_{affected} = 0.0016$,

792   independent of the size of the impactor. As R_C expresses the volume fraction of the silicate

793   that has reacted with the metal, it may overestimate the volume of the mantle that has

794   equilibrated with the metal phase. Hence the parameter R_C should be considered as a first-

795   order approximation of the volume equilibrated. Therefore, for Eq. (12), the mass of

796   mantle that is equilibrated is obtained by simple multiplication by $\rho_{mantle}.$ In this mass of

797   mantle, the concentration of Ni or Co is in equilibrium and is given by $\chi_{eq}^{silicate} =$

798     $\frac{\chi_{impactor}^{metal}}{D^{met/sil}}$. The final mass fraction of Ni or Co is given by:

799

800               $$\chi_{final}^{silicate} = \chi_{initial}^{silicate} + (\chi_{eq}^{silicate} - \chi_{initial}^{silicate})\frac{m_{equilibrated}}{m_{mantle}} \qquad (16)$$

801

802 where, $\chi_{final}^{silicate}$ is the concentration of Ni or Co in the final mantle, $\chi_{initial}^{silicate}$ is the initial

803 concentration of Ni or Co in the mantle, $\chi_{eq}^{silicate}$ is the concentration at equilibrium,

804 $m_{equilibrated}$ is the mass that is equilibrated and m_{mantle} is the mass of the Earth's mantle. The

805 final Ni/Co ratio is then derived from $\chi_{final}^{silicate}$ for Ni and Co. The results of calculations

806 for different viscosities as a function of the impactor radius are presented in Fig. 16.

807

808 Fig. 16 shows that a single impactor, even a large one, does not significantly affect the

809 Ni/Co ratio in the mantle. The maximum variation is 0.25 %, and is obtained for a large

810 impactor (1000 km radius) for a relatively high viscosity of the magma ocean (100 Pa.s).

811 For low viscosities (0.1 and 1 Pa.s), a metallic impactor weakly affects the Ni/Co ratio in

812 the mantle (less than 0.1 % change for a 1000 km radius impactor). Such a small variation

813 confirms that high spatial resolution models are not necessary even for large Pe_{mesh} values

814 obtained for low viscosities. For a relative error of 100% in the values of R_c , at a viscosity

815 of 0.1 Pa.s, it would only induce a variation in Ni/Co of between 0 and 0.2% within the

816 final model.

817 Eq. (16) shows that the final concentration is proportional to the volume equilibrated if

818 $\chi_{eq}^{silicate}$ is higher than $\chi_{initial}^{silicate}$. In this case, late accretion of a metallic impactor, which

819 yields a high metallic concentration in Ni and Co (similar to the Earth core concentration

820 given in McDonough, 2003); with a high equilibrium pressure, which yields low partition

821 coefficient values for Ni and Co, ($\chi_{eq}^{silicate} - \chi_{initial}^{silicate}$) is positive. The impactor is

822   metallic and rich in Ni and Co (5.2%wt and 0.24 %wt, respectively), and impacts a silicate

823   mantle with a BSE composition. Therefore, when the mass of mantle equilibrated is

824   higher, the variation in Ni or Co concentration compared to the BSE in the mantle is

825   higher. If the disequilibrium is high, the $m_{equilibrated}$ is low, and therefore there is less

826   variation in the Ni/Co ratio. As shown in Fig. 16, the amount of disequilibrium is higher

827   for a low viscosity magma ocean, as well as for small metallic impactors, and therefore

828   there is no change in the moderately siderophile element concentrations in the mantle

829   under these conditions. This means that, to have a significant effect on the moderately

830   siderophile element concentrations in the BSE, late accretion impactors need to be large

831   and impact a viscous magma ocean in order to increase the degree of equilibrium. Even

832   in this case, if the amount of Ni and Co in the impactor is not significantly higher than that

833   in the Earth's core, the change in BSE composition will not be significant, as illustrated

834   in Fig. 16.

835

836   **6. Discussion**

837   **6.1.   Earth accretion models and magma ocean properties**

838   In the previous section we characterized the effects of a late impact, negligible in mass,

839   composed only of a metallic phase. However, most of the disequilibrium happens during

840   accretion. Therefore, Eq. (16) is not relevant, at least not in this form, in the context of a

841   growing planet. Assuming that the mantle of the impactor and of the growing Earth is well

842   mixed before equilibration with the metallic fraction, we can define the concentration of

843   the post-impact mantle, $\chi_{post-impact}^{silicate}$. By modifying Eq. (16), and knowing the

844   composition of the impactor's metallic phase it is possible to calculate the composition of

845   a growing planetary mantle before it equilibrates with the metallic phase of the impactor.

846   It is given by:

847    $$\chi_{post-impact}^{silicate} = \frac{m_{mantle}}{m_{mantle}-m_{equilibrated}}\left(\chi_{final}^{silicate} - \frac{m_{equilibrated}}{m_{mantle}} \chi_{equilbrated}^{silicate}\right) (17)$$

848   Since $m_{equilibrated}$ is dependent on the size of the impactor core and magma ocean viscosity,

849   it is possible to calculate the composition of the mantle for a 90% accreted Earth hit by a

850   Mars-sized impactor (Moon-forming impact) as a function of the impactor's core radius

851   and viscosity of the magma ocean. Fig. 17 shows the corresponding results for comparison

852   with Fig. 16: in this case, the greater the degree of equilibrium, the lower the initial Ni/Co

853   ratio.

854

855   The results displayed in Fig. 17 show that it is possible to reach the same final Ni/Co ratio

856   for the Earth's mantle with drastically different properties of the impactor and the magma

857   ocean. From Fig. 17, two post-impact models can be derived:

858   -   A model with a low $R_{core}/R_{impactor}$ ratio and low magma ocean viscosity,

859   which yields a lower degree of equilibrium between metal and silicate. In this kind

860   of model, the composition of the Earth's mantle is more dependent on the

861   equilibrium conditions between the metallic phase and the silicate phase than on

862   the composition of the impactor. For instance, the models presented in *e.g.* Burbine

863   & O'Brien (2004), Rai & van Westrenen (2013) or Dauphas et al., (2014) are based

864   on mixing different chondritic compositions where the main parameter fitted is the

865   isotopic consistency, and they are therefore predominantly compositionally-

866   derived models. For these models to be consistent, the impactor's core needs to be

867   small ($R_{core}/R_{impactor} < 0.4$, left-hand side of Fig. 17), and the magma ocean

868   viscosity low ($\mu_{magma\ ocean} \approx 0.1$- 1 Pa.s), so as to achieve a low equilibrium rate

869   between metal and silicate.

870   -   A model with a high $R_{core}/R_{impactor}$ ratio, and high viscosity of the magma

871   ocean, which yields greater equilibrium between metal and silicate. In this kind of

872   model, the main changes in Earth mantle composition are due more to the

873   composition of the impactor and less to the chemical reactions between metal and

874   silicate. For instance, the models presented in *e.g.* Wood et al., 2008, Siebert et al.,

875   2012 and Boujibar et al., 2014 are based on the metal-silicate partitioning behavior,

876   where the discriminating parameter is the relative core/mantle abundances of

877   siderophile elements, and they are therefore predominantly equilibrium-derived

878   models. In this kind of model, a minimal equilibrium needs to be reached, and

879   therefore the impactor's core needs to be large ($R_{core}/R_{impactor} > 0.4$, right-hand side

880   of Fig. 17), and/or the magma ocean viscosity needs to be high ($\mu_{magma\ ocean} \approx 10$-

881   100 Pa.s).

882   To summarize, our results cannot constrain the viscosity of the magma ocean (especially

883   given the error in our calculations for low viscosity calculations, see Section 2.4), but for

884   a given model, our results can constrain the range of magma ocean viscosities in order to

885   reach the BSE concentrations for moderately siderophile elements.

886   However, this work needs to be done for each accretion step or impact, and for each

887   element, which would increase the number of plausible scenarios to accrete the Earth, but

888   could also provide compositional constraints on irreconcilable scenarios, and therefore

889   allow some impactor compositions to be excluded from a given model.

890

891   **6.2.   Effect of Moon formation on the Ni/Co ratio in the Earth's mantle**

892   In the previous section we showed that the properties of the magma ocean are model

893   dependent: they have to be inferred from the impactor properties and the final BSE content

894   chosen as a control of the model output. In this section, we infer the viscosity of a magma

895   ocean for one particular model: the Moon formation by an impact with a Mars-sized

896   impactor (Canup, 2004). The Moon forming impactor (named Theia) is believed to be a

897   large Mars-sized impactor which hit the proto-Earth at the end of accretion with an oblique

898   trajectory (Canup & Asphaug, 2001, Canup, 2004). In a simulation of this kind of impact,

899   most of the metal and silicate of the impactor merges with the Earth (Canup, 2004). If we

900   consider mass of the Moon to be negligible compared to that of Theia, and ignore the loss

901   of particles due to the impact, we can determine that the final 10% mass accreted to the

902 Earth was due to the impact with Theia. The core of this impactor is 30% of the total mass

903 of the impactor (Canup, 2004), with the same mean density as the Earth, so it is not

904 improbable that the ratio $R_{core}/R_{impactor}$ is comparable to that of the Earth or Mars today

905 (given by the red and blue vertical lines in Figs. 17). In that case, Eq. (17) and Fig. 17

906 shows that some equilibrium occurred between the magma ocean formed by the impact

907 and the impactor's core sinking into the Earth's core. For every magma ocean viscosity

908 tested here, it is necessary to have interaction between Theia's core and the proto-Earth's

909 mantle to get the final BSE concentration. For a magma ocean viscosity of 0.1 Pa.s, the

910 proto-Earth's Ni/Co ratio is between 0.25 % and 0.45 % lower than the BSE values for a

911 $R_{core}/R_{impactor}$ comparable to those of Mars and the Earth respectively. For a magma ocean

912 viscosity of 100 Pa.s, the proto-Earth Ni/Co ratio is between 1.45% and 3.00 % lower than

913 the BSE values for a $R_{core}/R_{impactor}$ comparable to those of Mars and the Earth, respectively.

914 This means that the Moon forming impact had a significant effect on the BSE Ni/Co ratio,

915 which can be high if the magma ocean formed after the impact was viscous (100 Pa.s) and

916 the core radius of Theia was around 1850 km.

917

918

919 **7. Conclusion**

920 We developed numerical models to characterize the effects of viscosity and partition

921 coefficients on the metal/silicate equilibrium for moderately siderophile elements. We

922   showed that the volume of silicate equilibrated with a small volume of metal is mostly

923   controlled by the partition coefficients and the viscosity of the silicate. The viscosity ratio

924   between metal and silicate is a second order parameter but still has a significant effect.

925   The scope of this study does not include other elements that have different partitioning

926   behavior (V, Cr, Mn etc.) and future models of equilibrium between metal and silicate

927   will have to integrate these elements to get a clearer view of chemical exchanges within

928   the Early Earth. Furthermore, the range of *Re* and *We* covered in this study does not cover

929   the whole range of *Re* and *We* numbers during the accretion event (Fig. 10). Therefore, in

930   the future, we will need to model more complex flows (such as shown in Samuel, 2012 or

931   Wacheul et al., 2014), to widen the scope of our interpretations (see Section 4 for the

932   extrapolation conditions). Future models should also account for the thermal equilibration

933   during metal/silicate separation (Wacheul & Le Bars, 2018) to characterize the effects of

934   temperature on the partition coefficient values. Other phenomena, while important, are

935   ignored due to being beyond the scope of the study, for instance the effect of the droplet

936   size and shape (Qaddah et al., 2019), or stretch-enhancing diffusion (Lherm & Deguen,

937   2018), or the possibility of large core-merging events (Landeau et al., 2016). All these

938   phenomena are beyond the scope of this study and should be taken into account in further

939   work and models of accretion.

940   Nevertheless, we proposed a parameterization of the disequilibrium between a silicate

941   magma ocean and a metallic droplet for moderately siderophile element behavior. Using

942   this parameterization on Ni and Co behavior at the end of accretion, it is possible to define

943   some constraints on the viscosity of the magma ocean. For a given model of accretion to

944   fit the current BSE concentrations, the viscosity of the magma ocean and the impactor

945   composition need to be changed accordingly: large impactors with large metallic cores

946   (R_{core} > 1100 km) and high magma ocean viscosity (10 -100 Pa.s) favor a high degree of

947   metal/silicate equilibrium; while metal/silicate disequilibrium models can be achieved

948   with moderately small metallic cores (R_{core} ≈ 300-1000 km) and low viscosity (0.1 - 1

949   Pa.s) magma ocean.

950   When applying our results to the Moon-forming impact, we showed that the current Ni/Co

951   ratio in the BSE is affected by the Moon's formation, depending on the viscosity of the

952   magma ocean formed after the impact. The Moon's formation can account for 0.25 to 0.45

953   % of the final BSE Ni/Co ratio for a low viscosity (0.1 Pa.s) magma ocean, and for 1.45%

954   to 3 % of the final BSE Ni/Co ratio for a high viscosity (100 Pa.s) magma ocean.

955

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Captions of Figures and Tables

Figure 1: Schematics of core-mantle segregation. First, the impactor (metal+silicate) enters a turbulent magma ocean. The impactor is fragmented and melted on impacting the surface of the proto-planet. The metallic phase then forms a diapir which, if the magma ocean is turbulent enough, fragments into a cloud of droplets ranging in size from a few millimeters to 10 cm maximum (Rubie et al., 2011; Deguen et al, 2014; Wacheul et al., 2014; Wacheul and Le Bars, 2017,2018). Each droplet interacts with the surrounding silicate, exchanging heat and chemical elements, until it reaches thermo-chemical equilibrium with its environment.

Figure 2: Schematic representation of the initial conditions and geometry of our models. The characteristics of the metal and silicate phases are listed respectively in red and black. The boundary conditions are detailed in blue (top), solid red line (side), green (bottom and global conditions). The red arrow illustrates the symmetry axis (red dotted line) used to define the 3D output.

Figure 3: Evolution of the metallic volume ratio ($V_{calculated}/V_{theoretical}$) during a simulation for different h_{max} values, for a silicate viscosity of 100 Pa.s. The colored and dashed line represent the evolution of $V_{calculated}/V_{theoretical}$ for different mesh sizes with time. The scale at the top shows the distance traveled by the diapir over a given time.

1237   **Figure 4**: Evolution of the velocity field, r-component (on the left) and z-component (on

1238   the right), for different widths of computational domain. Widths vary from 2x R_{Fe} to 6x

1239 R_{Fe}. The chosen width for the simulations is 5xR_{Fe}. Note that the results presented here

1240   are calibration runs, with a height of 30x$R_{Fe.}$ The same simulations have been performed

1241   at varying heights, leading to a final height of 28x R_{Fe} (see Fig. 2 for the calibrated

1242   geometry).

1243   **Figure 5:** Evolution of the volume fraction of the silicate during the simulation. When

1244   equal to 1 (red), the fluid is a silicate, when equal to 0 (blue) the fluid is a metal. The limit

1245   between metal and silicate is the black line between the red and blue parts ($\Phi_{ls} = 0.5$). The

1246   time necessary for the diapir to reach the distance of 10R_{Fe} is 12.1 s.

1247

1248   **Figure 6:** Evolution of adimensional concentration of the siderophile element in the

1249   silicate, for a partition coefficient $D^{met/sil} = 1$. For clarity purposes the metal is shown by

1250   the grey area surrounded by a black line. The black line is the boundary between metal

1251   and silicate and defines the surface where the exchange reaction happens. The

1252   adimensional concentration is given by the following formula given in Eq. (9). In this case

1253 $X^0_{sil} = 10^{-5}$, $X^0_{met} = 0.2$ and $D^{met/sil} = 1$, and the chemical Peclet number is Pe~800**.**

1254

1255   **Figure 7:** Evolution of the volume of silicate undergoing reaction during the simulation.

1256   In red, the volume of silicate affected chemically. In blue, the volume of silicate unaffected

1257   by the passage of the diapir. The metal is colored in grey. The ratio R_C defined in the study

1258   corresponds to the volume of the red areas divided by the total volume of silicate (red +

1259   blue areas).

1260

1261   **Figure 8:** Evolution of R_C as a function of time in the reference case defined in the text

1262   ($\mu_{sil} = \mu_{met} = 100$ Pa.s). The four lines illustrate four different values of $D^{met/sil}$ ranging from

1263   1 (black) to 10^3 (blue).

1264

1265   **Figure 9:** Evolution of the time necessary for the diapir to move through $10R_{Fe}$ as a

1266   function of the silicate viscosity. Black points are the values corresponding to each

1267   study. The red area corresponds to Stokes flows, and the blue area to intermediate

1268   flows. The clusters of black points correspond to the variation in velocity due to the

1269   variation in metal viscosity. The theoretical values are plotted in red and derived from

1270   equations (9) and (10). Typical times of diapir equilibrium, from Wacheul et al. (2014),

1271   are shown in blue. The size of the marker is scaled logarithmically on the chemical

1272   Peclet number, ranging from 8 (smallest) to 3000 (largest).

1273

1274   **Figure 10:** On the left: Re as a function of We obtained from our numerical simulations

1275   (one red circle for each calculation). The blue area shows the Intermediate regime flow,

1276   and the red area the Stokes regime flow. The dashed area illustrates the domain where

1277   diapirs are stable. On the right: Comparison between the geologically plausible values of

1278 We and Re for the Earth's magma ocean and the values covered by our study.

1279

1280   **Figure 11:** Evolution of R_C as a function of Re during the sinking of a 1cm-radius droplet

1281   for an adimensional time of 1. The Stokes flow regime (red area) and intermediate flow

1282   regime (blue area) are separated by a black vertical line at $Re=1$. The dot color

1283   characterizes different values for $D^{met/sil}$ ranging from 1 to 10^3. The size of the marker is

1284   scaled logarithmically on the chemical Peclet number, ranging from 8 (smallest) to 3000

1285   (largest).

1286   **Figure 12:** Evolution of R_C as a function of R_μ for 5 different metallic viscosities (shown

1287   in the 5 boxes), different values of $D^{met/sil}$ and obtained at a distance of $10R_{Fe}$. From top

1288   left to bottom panel the metallic viscosity increases from 0.1 Pa.s to 1000 Pa.s. The silicate

1289   viscosities corresponding to R_μ are indicated on the top x-axis. The size of the marker is

1290   scaled logarithmically with the chemical Peclet number, ranging from 8 (smallest) to 3000

1291   (largest).

1292

1293 **Figure 13:** Evolution of log R_C as a function of the normalized surface (left panel) and

1294 evolution of the normalized surface as a function of R_μ (right panel) for models with $\mu_{silicate}$

1295 = 0.1 Pa.s for the reference time defined in Fig. 9. The normalized surface of the diapir is

1296 the surface of the diapir in the simulation divided by $S_{theoretical} = 4\pi R_{Fe}{}^2$ (initial surface of

1297 the sphere).

1298 **Figure 14:** logRc calculated from the parameterization of Eq (11) vs logRc obtained from

1299 the simulations. The red line is the 1:1 line (perfect fit), and the dashed lines bound the 5σ

1300 confidence interval.

1301

1302 **Figure 15:** Mantle fraction chemically contaminated by a moderately siderophile element

1303 after metallic core fragmentation as a function of the impactor size. In these figures we

1304 compute Eqs. 6, 11 and 12 using R_{Fe}=1cm, $v_{diapir}=v_{stokes}$ and μ_{met}=0.1 Pa.s. The left panel

1305 shows the influence of the partition coefficient for a fixed viscosity ratio R_μ=1. The right

1306 panel shows the influence of the viscosity ratio for a fixed partition coefficient

1307 $D^{met/sil}$=100.

1308

1309 **Figure 16:** Evolution of Ni/Co ratio in the mantle after an impact as a function of the

1310 impactor size for different silicate viscosities (0.1 to 100 Pa.s). We represent here the

1311 variation of the Ni/Co ratio after the impact relative to the initial BSE concentration:

1312 $\Delta\left(\frac{Ni}{Co}\right) = 100 \times \frac{(\frac{Ni}{Co})_{Final}-(\frac{Ni}{Co})_{BSE}}{(\frac{Ni}{Co})_{BSE}}$. Since the impact happens on the BSE, the more the

1313 Ni/Co ratio is different to that of the BSE, the more the impactor has reached equilibrium.

1314

1315 **Figure 17:** Ni/Co ratio in the Earth's mantle before equilibration with the core of an

1316 impactor corresponding to 10% of the Earth's mass as a function of the radius of the

1317 impactor's core normalized to the impactor size and for different magma ocean viscosities.

1318 The R_{core}/R_{Earth} current ratio is shown by the blue dashed line, and the R_{core}/R_{Mars} ratio by

1319 a red dashed line. In the calculation, the impactor is the same size as Mars ($R_{impactor} = 3390$

1320 km), and the impactor core radius ranges from 340 km to 2040 km. We represent here the

1321 variation in Ni/Co ratio before the impact relative to the BSE concentration but for a well-

1322 mixed mantle after impact: $\Delta\left(\frac{Ni}{Co}\right) = 100 \times \frac{(\frac{Ni}{Co})_{post-impact} - (\frac{Ni}{Co})_{BSE}}{(\frac{Ni}{Co})_{BSE}}$.

1323

1324 **Table 1:** Parameters and variables used in this study. When values are not given, the

1325 variable is calculated later in the text (according to the specific case).

1326

1327 **Table 2**. Values of fitted parameters for Eq. 11 using the least-square methods. The errors

1328 associated with the value are given by the 1σ error value. The data used for

1329 parameterization are the same as the data presented in sections 3.3 and 3.4. The

1330 comparison between calculated values from Eq. 11 and the values obtained after

1331 simulation is presented in Fig. 13.

1332

1333 **Table 1**

Parameter	Name	Values in this study
All models		
ρ	Density of the fluid	silicate: 3300 - metal: 8000 kg.m^{-3}
t	Time	0.6 - 125 s
u	Velocity vector	m.s^{-1}
R$_{Fe}$	Radius of the diapir	1 cm
h$_{max}$	Maximum unit cell size	**0.1** $\times$ R$_{Fe}$
Two-phase flow		
P	Dynamic Pressure of the fluid	1 atm
μ	Dynamic viscosity of the fluid	$10^{-1} - 10^3$ Pa.s
g	Acceleration of gravity	9.81 m.s^{-2}
l	Distance fluid - initial interface	m
F_{st}	Surface tension force	Calculated for σ = 1 N.m^{-1}, in N.m^{-3}
Φ	Volume fraction of the fluid	silicate: Φ =0 metal: Φ = 1 no unit
ϵ_{ls}	Parameter controlling interface reinitialization	h$_{max}$/2

	Parameter controlling velocity reinitialization	$0.001 - 0.3$ m.s^{-1}
γ		
Transport of Diluted Species		
c_i	Concentration of element i	mol.m^{-3}
k_c	Diffusion coefficient of element i	10^{-6} m^2.s^{-1}
R_i	Reaction rate for element i	mol.m^{-3}.s^{-1}
N_i	Molar flux of element i	0 mol.m^{-2}.s^{-1}
Scaling of the study		
Re	Reynolds number	2.5×10^{-5} to 110
We	Weber number	2.3×10^{-5} to 3.5
R_μ	Viscosity ratio ($= \mu_{met}/\mu_{sil}$)	10^{-4} to 10^4
R_C	Ratio of the silicate volume reacted	see Section 3

1334

1335 **Table 2**

Parameters	a ($Dmet/sil$)	b (Re)	c (R_μ)	d
Values	-0.235	-0.283	0.011	-1.686
1σ	0.02	0.03	0.001	0.07

1336

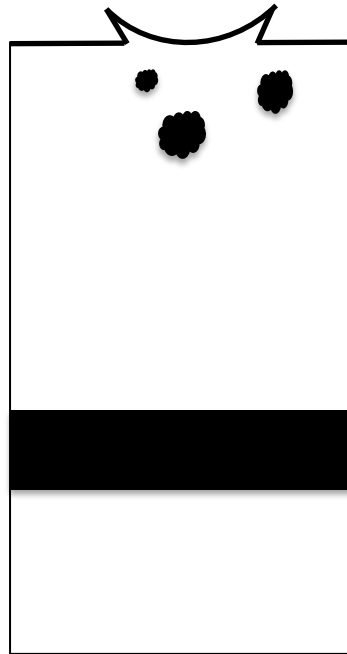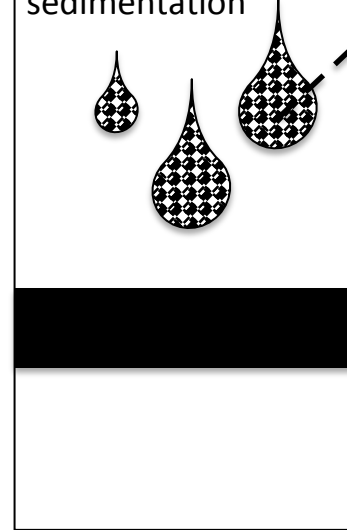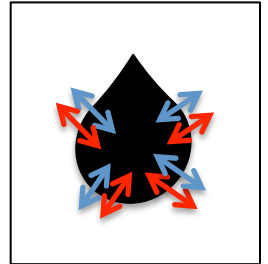Turbulent Magma ocean

Ponded metal layer

Viscous early mantle

Impact fragmentation

Cloud sedimentation

Iron droplet

Thermo-chemical exchanges

Figure axes:
- x-axis: **logR_C calculated in simulations**
- y-axis: **logR_C parameterized**

Legend:
- ● logR_C parameterized
- ── 1:1 line
- --- 5 σ