Technical Report: 3D mesh Segmentation Application to glasses
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Abstract

Object segmentation in meaningful parts is an important research topic as these have become a part of many mesh and object manipulation algorithms in computer graphics, geometric modeling and computer aided design. In particular, tasks that were before realized by experts are more and more assumed by people without particular formation in geometric or computer graphic problems. So there is a need to have some ergonomic tools that have expert know-how while user keep control on specific constraints to its particular application. Here, we present how for segmentation purpose we model expert know-how and two algorithms that can be used to make segmentation task. One is generic and the other is specialized for glasses segmentations.

1 Introduction

In reason of 3D printers democratisation and easy access to 3D scanners, there is more and more 3D meshes available on internet. So use of 3D mesh becomes commonplace, increasing needs in automatic processings and in interfaces for
computer-aided manipulations. In particular, tasks that were before realized by experts are more and more assumed by people without particular formation in geometric or computer graphic problems. So there is a need to have some ergonomic tools that have expert know-how while user keep control on specific constraints to its particular application. Mesh segmentation has become a key point in many computer graphics tasks and applications and also in geometric modelling. Segmentation can help for parametrization, mesh editing or animation and many other tasks [4, 5]. So segmentation is a crucial point when we want to offer tools for automatic processing.

Mesh segmentation partitions the surface into a set of clusters under some criteria often depending of the final application. Comparative survey on segmentation technics [11, 16, 24] classify them in two categories: geometric segmentation and semantic segmentation. We are only interesting in the second one: our aim is to extract meaningful parts (having experts knowledge about what that mean) of an object in reasonable time, as it will be a pretreatment in a more complete application. Different parts should be well identify because different treatment will be allowed depending on their nature. Automatically identify meaningful parts of a 3D mesh is challenging. A common practice is to build some specific features by extracting some geometric or volumetric properties like approximate convexity analysis [8], concavity-aware field [2], spectral clustering [12], K-means [18], core-extraction [9], graph-cuts and randomized cuts [6], randomwalk [11] and then use it for segmentation purpose. Part boundaries or frontiers are faces which have at least one neighbor with a different label (that is which belongs to another part than theirs). Inducing part boundaries along negative curvature minima is often used even for semantic segmentation because they often offer natural separation between parts like legs and torso. Volumetric considerations can also be used and are more related to skeletal shape representation like shape diameter function [17].

Rathers than trying to segment a single object some recent researches are done on co-segmentation [7, 13, 19, 20, 25]: the aim is to segment in the same time a family of objects (for example different glasses) because more semantic knowledge can be extracted by simultaneously analyzing a set of shapes instead of a single shape. But their final objective is slighly different of ours as they only guarantee consistent segmentation over the set whereas we want to use expert knowledge about what is for a given problem a good segmentation. Indeed, often saying what is meaningful parts or good segmentation is not a so easy task. Good exemples of that can be found in [5] where users are asked to segment different objects. We can see that different persons segments same object differently (see figure 1). Why one should be consider better than another?

That why, we consider that we have at least an exemple of good segmentation in the sense that it has be done by an expert and so it can be considered well-suited for its specific problem. In consequence, here, expert knowledge will be represent by at least one shape and its good segmentation and our aim will be : given another shape of the same family, how can we segment it so that extracted meaningful parts are coherent with example shape.
2 Strategy

2.1 Context

Our project implies at the same time a local company Polymagine and a research laboratory LIMOS. Company needs directed areas of research so that proposed solutions can be used in industry in the long run. In particular, we will take care about time computations and will try to have few constraints for meshes (we will not fix number of vertices or faces for example). Polymagine is specialized in personalisation of objects. Polymagine is interesting in segmentation as a pre-processus before personalisation step: deformation and transformation cannot be apply in the same way on all the object. They represent the expert knowledge and provide us some segmentations examples for glasses (see figure 2). So, glasses are for us composed of tenon (in red) on which will come to hang on the legs of glasses, circles (in blue) which hold glasses and finally bridge (in green) which connects both circles. We assume that we have at least one labelled example of glasses but not a lot.

Figure 1: An exemple of segmentations of the same objet, here glasses, from different persons. Segmentations can be found in [http://segeval.cs.princeton.edu/](http://segeval.cs.princeton.edu/) details of segmentations process are described in [5].

Figure 2: *Good segmentation* of glasses. Tenons are in red, circles in blue and bridge in green.
2.2 Learning with (deep) neural network

Deep learning is widely used in image segmentation process. AlexNet [10] is one of the more known deep neural network. It is one of the pioneer in deep CNN. Visual Geometry Group (VGG) [21] and GoogLeNet [23] are two others very well known deep neural network for image segmentation. They give good results. Even if CNN (Convolutionnal Neural Network) cannot be used for mesh segmentation because of the complexity of 3D geometry (a vertice don’t have all the time the same number of neigboor whereas in an image the number of pixels surrounded one pixel is fixed), it seems to us that neural network can be interesting in our case, as we want to transfer knowledge from given examples to new examples of same family.

2.3 Features

When using neural network, what are entries is one of first question to answer. As previously stated, vertices (or faces) of meshes are not good candidates because they can vary in number and it is difficult to order them : what can be consider as first vertice and how we traversed the others ? So we make the choice to work as in more classical mesh segmentation technics with particular features.

We find that the work of [25] is interesting. Their aim is not exactly the same as they want to make co-segmentation and so do not have a model to respect in segmentation. They compute presegmentations (rough segmentations) of a family of meshes using K-means in space of eigenfunctions of Laplace-Beltrami [3, 14]. Then they use these presegmentation and properties of Laplace-Beltrami operator to compute Functional Maps [15] and to make correspondance between parts of differents objects. Then, they are able to make segmentation of their family of meshes. Results on differents family of shapes are impressive.

We make some preliminary tests using the code for Functional Maps provided on [http://www.lix.polytechnique.fr/~maks/fmaps_course/publications.html](http://www.lix.polytechnique.fr/~maks/fmaps_course/publications.html). To use this code, we need to have a pre-segmentation of meshes, that is a segmentation in some coarse regions and we need meshes with the same number of vertices. This two conditions are for us only for tests, because we want to be able to treat meshes from our industrial partner that will not respond to this criteria (meshes tend to have the same order of vertices but not exactly the same number).

On figure 3 tree pre-segmentations are showns. On figure 4 results of Functionals Maps given the previous pre-segmentation are shown. Colors indicates similar regions. On the first sub image, the second glasses (the upper one) has been created by deformation of the first glasses (on bottom). Matching between the two shapes is not perfect in particular near the bridge but it seem to be promising. At contrary, on second subimage, the two shapes have independant meshes and matching is really bad.

Functional Maps not seem to be well-suited for our problematic were meshes are not near isometric deformation one from another. Nevertheless, we keep
Figure 3: Pre-segmentations for tree different glasses: glasses a), glasses b) and glasses c).

Figure 4: Functional Maps used on our glasses. First column shows front of glasses and second columns the back. First rows is between glasses b) and a). Second rows is between glasses a) and c). Same colors should indicate correspondent regions.
being interesting in the Laplace-Beltrami Operator as features. Indeed Laplace-Beltrami is a local descriptor where different feature information are represented by different feature functions. Since eigenfunctions of Laplace-Beltrami are order from low-frequencies to high-frequencies. Yet low-frequencies contain more information than high-frequencies functions. So a few of Laplace-Beltrami eigenfunctions can be used as features descriptors. Advantage of Laplace-Beltrami eigenfunction are that they are independant from shape spacial localisation and that it describe well shape geometry. In figure 5, the 4 first eigenfunctions of Laplace-Beltrami are shown.

On experiments, there can be some problems of flips in Laplace-Beltrami eigenfunctions : sometimes sign of similar regions are inverted. An exemple is given on figure 6. On the first glasses, high value (in yellow) are on bottom-left circle and upper-right circle whereas on the second glasses it is on bottom-right circle and upper-left circle. To overcome this problem of flip signs, we simply consider the absolute value of the Laplace-Beltrami eigenfunctions. We will also normalize eigenfunction to be between 0 and 1 :

\[ \phi_i^* = \frac{|\phi_i| - \min_j |\phi_i(x_j)|}{\max_j |\phi_i(x_j)| - \min_j |\phi_i(x_j)|} \]  

where :

- \( \phi_i^* \) : is the \( i \)th feature used. It is the \( i \)th eigenfunction of Laplace-Beltrami in absolute value and normalized.
- \( \phi_i \) is the \( i \)th eigenfunction of Laplace-Beltrami.
- \( x_j \) is a vertice of the mesh
- \( \ | - | \) represents the absolute value.

In fact, we are more interested in having one label per face than having one label per vertice so we convert this vertice features in face features. To make
that, for a face $f$, we consider the 3 vertices which compose it (as we work on triangulated mesh) and we say that the feature face value is the mean of the 3 features vertices.

$$\phi^*_i(f_k) = \frac{1}{3} \sum_{j=1}^{3} \phi^*_i(v^k_j)$$

(2)

where:

- $\phi^*_i(f_k)$ is feature vector computed for face $f_k$ and we will refer to it by absolute-normalized eigenfunctions of Laplace-Beltrami for face $f_k$.
- $\phi^*_i(v^k_j)$ is the absolute-normalized eigenfunctions of Laplace-Beltrami for a vertice $v^k_j$ that is one of the 3 vertice of the face $f_k$.

By default, when we will refer to this face feature, we will named these absolute normalized eigenfunctions of Laplace-Beltrami (and we will ommitted for face).

Another problem with the Laplace-Beltrami eigenfunction is an ordering problem: even if all regions can be well characterized by these functions, sometimes it is not the same function that represent correspondent regions. Whereas sign flip can be easily removed by taking the absolute value of eigenfunction, there is no solution for this ordering problem. Or order has big importance when we want to use neural network. A node should always represent the same component. Or if there is change in order, it will not be possible. An exemple of this problem is illustrate in figure 7. For illustration purpose, we have change objects and show images on animals but problem is the same on glasses. Here, leg regions are represented one time by the 3rd eigenfunction of Laplace-Beltrami and on other on the 4th eigenfunction.

2.4 Construction of our neural network

To construct our neural network, we have to take into account to the previous remarks and to industrial time constraint: we want that segmentation process can be used in some application so that should not take to much time. As we are only developing some prototype, a time of few minutes (5 minutes should be the maximum and if possible less than one minute) is the goal fixed by Polymagine, considering this computation time could be improved if technics give good results.
Another important constraint is that we want to treat any mesh given so number of vertices or faces cannot be fixed and our neural network must be able to work with. Often, when size of example if not fixed, RNN (Recurrant Neural Network) are used, in particular for text recognition. But, we think it was not suitable for us, as a sequence has natural order: place of words in sentence (or place of letters in words) are important: verb is after subject and so on. In meshes, ordering is difficult, there is no natural beginning or end of meshes. That why, we decide to take in entry only feature for one face. Doing this, all size of meshes can be treated, if a mesh has $n$ faces, we simply need to use $n$ times our neural network only changing entries. As we give only one face after another, we cannot ensure topological consistence from neural network but we think that absolute-normalized eigenfunctions of Laplace-Beltrami contain enough information about face neighbourhood to ensure coherent segmentation.

The main problem that remains is an ordering problem. As discussed previously, absolute-normalized eigenfunctions of Laplace-Beltrami can have different order in different meshes. So we cannot make training on some glasses and then used trained neural network on new glasses. Our main idea, that is really different from usual use of neural network, was that we do not need to learn on a lot of faces and that only few faces can be used to make training. Idea is to have for one particular mesh few labelled faces per class that are well positionned and to transfert this face (like some initial source seeds) to another glasses. Once, we have for new glasses, some labelled faces we can make training with our features faces for new glasses on this few labelled faces (on new glasses) and then we only need to used the trained neural network on all faces of new glasses. As training is on features from new glasses, there is no problem of order (in one mesh, order is always consistent).

With this idea, we choose to construct a neural network with only one hidden layer considering that as we want to train with few data, we will not have enough data to learn a lot of weighs in a lot of hidden layers. The other good point, in having a small neural network is that training step will be fast (as testing step). We have a fully connected neural network with 50 entries (the 50 first absolute normalized eigenfunctions of Laplace-Beltrami) , 3 outputs (one per class) and
250 nodes on hidden layer. Activation functions from entries to hidden layer are sigmoids and activation functions from hidden layer to output are softmax functions.

3 Method 1 : Seed Transfert

In this section, we will present in more details our method using the previous idea.

3.1 First Tests

During the analysis phase, we made hypothesis and thus first step is to verify them. We begin by trying to learn segmentation on mesh when we manually select the seeds. Good selection of seeds imply :

- every class should have the same number of seeds. Seeds must be balanced in number.
- in every class, seeds must be spatially distributed. Seeds should be as far away from other seeds of same class as possible.
- in every class, some seeds must be near boundaries : if we segment every face in mesh, some seed must be near a face of different label (this face is not necessary a seed even for the other class).

We compute for all face of meshes, absolute-normalized eigenfunctions of Laplace-Beltrami. We use 10 seeds per class (for a total of 30 seeds) to train our neural network and after we use the trained neural network for testing segmentation on all faces. Figure 8 shows results for one glasses. Segmentation is coherent with what we want and so it seems that our idea can work.

3.2 Seeds Transfer

To have an automatic process, we want to have an algorithm that is able to transfer seeds from source mesh (we know source seeds labels) to target mesh.

Figure 8: Segmentation from manual seeds using our neural network
We want to label the same number of faces in target mesh than in source mesh. Labelled faces in taget mesh will become seeds for target mesh.

### 3.2.1 Distance Transfer

Firstly, we consider we have aligned glasses. Under this hypothesis, transferring seeds can be seen as a research of $k$-nearest neighbour where $k = 1$, tree is constructed using target mesh face (the center of face is taken as 3D point), query points are center of seeds in source mesh. The target face that is selected become a seed for target mesh with same label as source seed.

### 3.2.2 Distance Transfer + eigenfunctions

As glasses have not all exactly the same shape, distance transfer can be improved by taking into account more topological information. For every seeds in source mesh, we will find the $k$-nearest neighbour where $k = 250$. This ensure a spacial coherence. But after to select the final target face, we compute distance between the 3 first eigenfunctions of Laplace-Beltrami, the face with the lower distance is kept as target seed. The idea is that eigenfunction of Laplace-Beltrami will probably be more similar on place that have similar function in glasses.

Results of the two transfer can be seen in 5.1.

### 4 Method 2 : Training

We are also interesting to see if we can use our neural network to make some more usual training as the context change a little bit and more labelled glasses are available. Like we previously discuss, using absolute-normalized eigenfunction of Laplace-Beltrami is not suitable for this purpose so we have to change our features.

We choose to use HKS (Heat Kernel Signature) [22]. As previously, we will take it in absolute value, normalize it and compute a mean to have features for face. So we will named it absolute-normalized HKS. We believe theses features will be less sensitive to the ordering problem. We choose to take 50 features.

We used $k$ glasses to make training. On every glasses we randomly select $n$ faces for every class. So we have $kn$ examples in training set. We train our neural network (the one described in 2.4) only one time with these examples (training can be long). After, we compute for every new glasses, its absolute-normalized HKS features and use the trained neural network on every face by changing entries. Results are shown in 5.2.

### 5 Results

In this section, we will present some results obtained from the two methods. To implement our algoritahmes, we use Matlab to compute generalized eigenvectors and values, Tensorflow in Python to construct, train and use neural network and
C++ to compute features on mesh and make file readable by Matlab or Python. For a mesh with near 23914 vertices and 47832 faces, we need to:

- compute mass matrix and cotangent matrix : 1.4 s
- compute generalized eigenvectors and eigenvalues : 21.6 s
- select seeds 4.9s using distance only or 7.6 s using distance + eigenfunctions
- compute normalized-absolute eigenfunctions of Laplace-Beltrami using previous steps and writing file test : 12s
- train our neural network : 3.4s
- use trained neural network on all faces : 6.5s

5.1 Result for the first method

Conditions: on one glasses, 10 faces (seeds) per class are well selected. Selected face are well balanced in every class region and somme of them are near boundaries. All meshes are aligned. As describes in section 3.2 we use two methods for transfert. The first one take into account only euclidean distance between faces, the second one select for each source face, the 100 nearest target faces and among this 100 target faces, the one with the most similar 3 first eigenfunction is chosen.

Figure 9 shows one case of mislabelling in transfert in both methods. On the left, it is the distance transfert and on the right it is the distance + eigenfunction transfert.. We can see error in labelling in left tenon, more visible in the second line.

In figure 10 we compare the results on both transfert on 12 glasses. First column represents results using transfert with distance only (and after training with seeds and testing) and second column represents results using transfert with distance and eigenfunction (and after training with seeds and testing). Results with distance and eigenfunction give a little bit better results. But two are not perfect segmentation and some glasses are bad segmented. The problem comes from error in labelling as first cause, and position of labelled seeds : they are not as well balanced as in source mesh (they can be less distant or it can lack of seed near boundaries).
Figure 9: Example of transfert labelling. In light grey it is not labelled face, in blue, it is tenon faces, in green bridge faces and in red circle faces. First line show labelled faces on full mesh and second line is a zoom on the left tenon to show error in labelling process. First column is labelling using transfert with only distance. Second column is labelling using transfert with distance and eigenfunctions.
Figure 10: First column represents results after transfer with distance only, training and testing. Second columns represent results after transfer with distance and eigenfunction, training and testing.
5.2 Result for the second method

Conditions: we use one glasses as training glasses. We consider we have a good segmentation for all the faces of the mesh. Among this faces, we randomly select 750 in every class, no particular care is done about the repartition of selected faces. Absolute-normalized HKS is computed for each face of all the meshes we want to test. Computing it take 72.3 s. Neural network is the one described in §2.4. Training take 196 s.

In figure 11, the result on the training glasses is shown. Mesh has near 25000 faces. Note that, segmentation is good even if we have train with only 2250 faces.

In figure 12, results on 12 others glasses are shown. Even if segmentation are not perfect, they are interesting and should be improved by modification on training: we can use more than one glasses and we also can select faces in a better way, maybe trying to have a good repartition on class as in the first method.

Figure 11: Result of segmentation on training glasses for the second method (general training + HKS).
6 Conclusions

In this report, we presented two algorithms for mesh segmentation using Laplace-Beltrami Operator to compute interesting features and neural network to learn from examples.

6.1 First Method: Seed Transfert

The first method transfers few seeds (a dozen per class is enough) from a source glasses to a target glasses. Seeds must be distributed among faces of similar class and some must be close to faces of others class (so near border of semantic region). Two methods of transfert are proposed. Both consider that glasses are aligned. The first use only euclidean distance between source face and target faces to affect a label. The other assume that there is no problem of order between the three first eigenfunction of Laplace-Beltrami. The 100 nearest faces in target mesh of a source face are selected and in these pre selected face, the one that has the most similar eigenfunctions is chosen.

Once seeds have been transferred, a neural network is trained. In entries, we used the 50 first absolute-normalized eigenfunctions of Laplace-Beltrami, and we have 3 outputs (one per class) that are used to affect label. There is only one hidden layer as we train we very few data (only 10 examples per class). Once the neural network is trained, for each face, we compute the absolute-normalized eigenfunctions of Laplace-Beltrami and use the neural network with this entry.
Si if a mesh have $n$ faces, the neural network will be used $n$ times. All this process take near one minute and computed time can be optimized. So it can be used for industrial purpose.

Having good initial seeds give good segmentation. For the moment, results are promising but need to be improved. The limitation step is in the process of transferring seeds. For industrial application, it is possible to imagine to have some graphical interface and let the user select seeds. The main advantage of this manual selection is that the quality of the seed should be better and so will lead to better segmentations. Another advantage is that with this manual selection no more alignment will be required. The main inconvenient is that ask more work from users.

6.2 Second Method : Big Train then Test

The second method use absolute-normalized HKS as features. The neural network is the same as previously but it is trained only one time with more examples (we have tests with 750 examples per class chosen on only one glasses but taking more examples and more glasses should improve results). The training step can be long but it is done only one time at the early beginning. After the training step, all we need is to compute absolute-normalized HKS for each face and use the neural network with these features in entry. We obtain segmentation for others glasses. The process (without training) take less than two minutes and computed time can also be improved. So this method can also be used for industrial purpose.

For glasses, it seems to be very promising but there is some restrictions to keep in mind. The first is that HKS is sensitive to size of meshes because of the use of eigenvalues, so object should be at the same order of size. The second restriction is the application to others objects: using HKS decrease order problem in eigenfunction of Laplace-Beltrami but do not solve all the problems. So, this method will not necessary give results for other shapes.

6.3 Conclusion and future works

We have developped two methods that can make segmentation using expert knowledge in particular case of glasses segmentation. Both methods can be used for industrial purpose as the time they need is low and can be improved. Both methods are promising but results are not exploitable for the moment and need more developments. One method should be generalized to other shape if we can improve the seed transfert. The other method will maybe give better results with less research but is probably suitable only for particular case.

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